Slab rollback instability and supercontinent dispersal

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Abstract Supercontinents coalesce over subduction zone complexes and their subsequent dispersal is usually attributed to heating and upwelling of continent-insulated mantle. This dispersal mechanism, however, requires considerable mantle internal heating. Alternatively, the supercontinent configuration may be mechanically unstable and disperse regardless of heating mode. In particular, increased drag on plates or subducting slabs (e.g., by accumulating continents) causes them to slow down and trenches to rollback. Once subcontinental slabs are slightly separated, resistance to their descent increases, inducing further trench migration. Slabs thus undergo a rollback instability, which disperses supercontinents. A simple theoretical model illustrates this instability and shows that there are two equilibrium states, one unstable supercontinent state where slabs are conjoined and one stable state where slabs are widely separated. Slab rollback from the unstable to stable states occurs at typical slow tectonics speeds and over a period commensurate with the age of ocean basins and the Wilson cycle.

1. Introduction

The Wilson Cycle is one of the basic tenets of plate tectonic evolution and describes the process of supercontinent agglomeration and dispersal [Wilson, 1966]. The driving mechanism for this cycle is traditionally attributed to the accumulation of continental crust over mantle downwellings (or complexes of subducting slabs) and the subsequent heating of the subcontinental mantle because of supercontinent insulation, which eventually drives an upwelling that disperses the supercontinent [Anderson, 1982; Gurnis, 1988; see also Yoshida, 2010, 2012, 2013; Yoshida and Santosh, 2011; Lenardic et al., 2011; Rolf and Tackley, 2011; Rolf et al., 2012, 2014]. This scenario, however, relies on active internal heating of the mantle by radiogenic sources [e.g., Gurnis, 1988; Lenardic et al., 2011; c.f., Yoshida, 2013; Rolf et al., 2014]. If the mantle energy source is primarily from primordial heat, i.e., its Urey number is very low [Korenaga, 2008; Jaupart et al., 2007], then the heating of the subcontinental mantle could be too weak to induce dispersal [e.g., Heron and Lowman, 2011].

We propose an alternative hypothesis for supercontinental dispersal that is independent of mantle heating mode. In particular, a major convergence zone drawn together by a large complex of downwellings is potentially unstable for purely mechanical reasons. First, divergent stress associated with thick continental crust opposes lithospheric convergence and slows plate motion, which causes the downwelling slabs to recede from each other, since the plates cool and become heavier closer to their spreading centers. As subcontinental slabs become more separated, the mantle between them induces greater viscous resistance, slows the slabs, and plates further, hence causing further rollback. The plates and slabs, therefore, undergo a rollback instability, which disperses the supercontinent. In this paper we illustrate the physics of this supercontinent rollback instability with a simple theoretical model and show that the predicted speed and time scale for dispersal are commensurate with the Wilson cycle.

2. Theory

Conditions for slab rollback have been studied extensively by Stegman et al. [2006, 2010] [see also Schellart et al., 2007, 2008; Clark et al., 2008], and while rollback form and evolution depends on plate strength, trench width, coupling to the overriding plate, and induced 3-D (especially toroidal) flow [Kincaid and Griffiths, 2003; Fucile et al., 2006; Piromallo et al., 2006; Stegman et al., 2010; Gerya and Melnik, 2011], a fundamental cause for rollback is excess negative buoyancy of the subducting plate [Stegman et al., 2010]. Here we develop a simple analytical boundary layer model to illustrate the supercontinent rollback instability. In particular, we show how slab and plate velocity are affected by the supercontinent configuration, which in turn alters the plate's negative buoyancy, convective stability, and, ultimately, its length.
We consider a simple configuration of two mirror-image sinking slabs (Figure 1), with symmetry points below the ridge at $x = 0$ and at the mutual convergence point $x = D$, where we assume the total cell width equals the mantle thickness $D$. The length of the plate to the slab is $L$, the slab width is $\delta$, and once the slabs separate, the gap between them has half-width $\lambda$. Although $L$ and $\lambda$ are time dependent, we require $L + \delta + \lambda = D$.

2.1. Plate Length and Trench Position

In our idealized model, subduction occurs where the top thermal boundary layer or plate goes convectively unstable. (The lithosphere is not considered inordinately strong since we assume some preweakening or self-weakening and/or damage mechanism [Bercovici and Ricard, 2012, 2014] has made it pliable enough to subduct [e.g., Gurnis et al., 2004; Nikolaeva et al., 2010]). The subducting slab thickness $\delta$ is given by equating the local Rayleigh number of the boundary layer to the critical Rayleigh number for the onset of convection [Howard, 1966; Solomatov, 1995]:

$$\frac{\rho g \alpha \Delta T \delta}{\mu_0 \kappa} = R_c$$

(1)

where $\rho$ is mantle density, $g$ gravity, $\alpha$ thermal expansivity, $\Delta T$ the lithospheric temperature drop, $\mu_0$ the upper mantle viscosity (which first resists the instability), $\kappa$ thermal diffusivity, and $R_c \approx 660$ is the critical Rayleigh number for a free-slip surface [Chandrasekhar, 1961]. Although $\delta$ is a system constant, it is related to plate age by $\delta = 2 \sqrt{\kappa L/w}$ [e.g., Solomatov, 1995] and thus the plate length is

$$L = \frac{\delta^2 w}{4 \kappa}$$

(2)

where $w$ is the slab's descent velocity, which is assumed the same as the plate velocity. Although subduction on Earth is more complex than implied here, and indeed there is a wide distribution of subduction ages [e.g., Becker et al., 2009], the relation (2) captures the basic process whereby if the slab and plate slow down, the plate becomes heavier and the trench retreats.

2.2. Ambient Mantle Flow and Resistance

If the model slabs become separated by a gap, the flow of the mantle inside the gap and behind the slabs provide viscous resistance to slab descent. Widening of the gap increases viscous resistance; hence, the plates slow down and cause the gap to widen further.

We consider the resistance to vertical descent of just one of the model slabs, since the other slab is its mirror image. We treat the vertical flow as Poiseuille flow wherein the slab's velocity $-w$ imposes a no-slip boundary condition on either of the slab's vertical surfaces (on the plate and gap sides at $x = L$ and $x = L + \delta$), while the symmetry points (below the ridge at $x = 0$ or mutual convergence point $x = D$) involve reflecting boundary conditions. On either side of the slab the vertical velocity is given generically by

$$v_z = -w + \frac{1}{2 \mu} \frac{dP}{dz} (b-x)(b+x-2a)$$

(3)

where $\mu$ is the mean viscosity of the whole mantle, which is dominated by the lower mantle's value, $dP/dz$ is a nonhydrostatic pressure gradient driving mantle return flow induced by the downward slab flux, and $a$ and $b$ are the positions of the reflecting and no-slip surfaces, respectively (i.e., $dv_z/dx = 0$ at $x = a$ and $v_z = -w$ at $x = b$). For the mantle below the plate, $a = 0$ and $b = L$, and for the mantle in the gap between slabs, $a = D$ and $b = D - \lambda = L + \delta$. We assume that the pressure gradient is the same on both sides of the slab, i.e., due to build up of slab material at depth; moreover, this pressure gradient is determined by mass
conservation wherein there is no net vertical mass flux across any horizontal surface in the cell. Integrating the vertical velocity from \( x = 0 \) to \( D \), including that of the slab and both regions of mantle on either side of it, yields

\[
- \frac{1}{2 \mu} \frac{d \rho}{dx} = \frac{3}{2} \frac{D}{\lambda^3 + L^3} \frac{w}{x}
\]

(4)

2.3. Continental Accumulation and Resistance

We consider the accumulation of a finite 2-D volume of buoyant unsubductable continental “fluid” of thickness \( h \), density \( \rho_c \), and viscosity \( \mu_c \), wherein the continental mass collapses if the underlying convergence ceases. The equation for a viscous 2-D gravity current of thickness \( h \) with a free-slip surface and a no-slip base moving at a horizontal velocity \( v(x) \) is

\[
\frac{\partial h}{\partial t} + v \frac{\partial h}{\partial x} = \frac{\rho' g}{3 \mu_c} \frac{\partial}{\partial x} \left( h \frac{\partial h}{\partial x} \right) - h \frac{dv}{dx}
\]

(5)

[Huppert, 1982] where \( \rho' = (\rho - \rho_c) \rho_c / \rho \) is the isostatically reduced crustal density [Didden and Maxworthy, 1982]. We assume the continental gravity current has an approximately self-similar shape near the downwelling slab and is given by \( h(x, t) = H(t) f(\zeta) \), where \( \zeta = (x - L - \delta / 2) / R \) (i.e., to the left of the slab \( \zeta < 0 \)), \( H \) is the characteristic height, \( f \) is a dimensionless shape function, and \( R \) is the half-length of the current’s base (Figure 1). The current’s volume is conserved; thus, the half-volume (per unit length into the plane) \( V = H(t) R(t) \int_{-1}^{0} f(\zeta) d\zeta \) is a constant; we can define \( f(t) = \frac{1}{2} \) such that \( H(t) = V / R(t) \). As we will later consider perturbations to a steady state, we assume the shape \( f(\zeta) \) approximates that of the steady critical wedge in which the advection term on the left balances the gravity collapse (i.e., nonlinear diffusion) term on the right of (5); in this case, and satisfying the volume integral constraint on \( f \), we find \( f(\zeta) = \left\{ 1 + (1 + \zeta)^{1/3} \right\}^{-1} \), for \( \zeta < 0 \). Substituting \( h = f(\zeta) \) into (5), evaluating it near the center of the gravity current (\( \zeta \approx 0 \)) where we assume \( dh/dx = 0 \) and \( dv/dx \approx -w / \delta \), we obtain

\[
\frac{dR}{dt} = \frac{c \rho' g V^3}{\mu_c} \frac{1}{R^4} - \frac{w R}{\delta}
\]

(6)

where \( c = 2^{2/3} \rho_c / \rho \approx 0.18 \). The stress of the continental gravity current acting against the top of the plate is \( \tau_c = -\rho' g h \frac{dh}{dx} \) and the force (per unit length into the plane) acting against the plate is

\[
F_c = \int_{L+\delta/2}^{L+\delta/2-R} \tau_c dx = -\frac{8 \rho' g V^2}{9 R^2}
\]

(7)

2.4. Mechanical Work Balance

The evolution of plate length is inferred from the balance of mechanical work on the slab; i.e., the release of gravitational potential energy of the slab is balanced by viscous work done by the mantle on either side of the slab and by the drag of the continental pile against the plate. In equilibrium, the steady subduction rate \( w \) allows for this energy balance. But if the trench recedes at a rate \(-dL/dt\), then the slab swings down and drops a distance \(|dL|\) in time \( dt \) and releases additional gravitational energy. The total energy balance is

\[
\rho a \frac{1}{2} \Delta T \delta \left( w - \frac{dL}{dt} \right) = \mu w \left( \frac{d\nu_c}{dx} \right)^{L+\delta} \left( \frac{1}{L} + \frac{1}{2} \right) \left( \frac{dL}{dt} \right)^2 - \frac{1}{D} \int_{L+\delta/2}^{L+\delta/2-R} \tau_c v_c dx
\]

\[
= 3 \mu \frac{D(D - \delta)}{\lambda^3 + L^3} w^2 + 2 \gamma \mu \frac{D - \delta}{L \lambda} \left( \frac{dL}{dt} \right)^2 + \frac{8 \rho' g V^2}{9 D R^2} w
\]

(8)

where \( \Delta T / 2 \) is the slab’s mean thermal anomaly, and we assume the plate velocity \( v_c \) is constant up to the trench and equal to the slab velocity \( w \). The fraction \( \gamma \) accounts for how much of the mantle is involved with rollback dissipation; e.g., if portions of the slab are anchored in the lower mantle (e.g., due to higher lower mantle viscosity), then they participate less in rollback, in which case \( \gamma \) is small.
Table 1. Material and Model Properties

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Symbol</th>
<th>Value</th>
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<tbody>
<tr>
<td>Density, mantle</td>
<td>( \rho )</td>
<td>3300 kg/m³</td>
</tr>
<tr>
<td>Density, continent</td>
<td>( \rho_c )</td>
<td>2700 kg/m³</td>
</tr>
<tr>
<td>Gravitational acceleration</td>
<td>( g )</td>
<td>10 m/s²</td>
</tr>
<tr>
<td>Thermal expansivity</td>
<td>( \alpha )</td>
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</tr>
<tr>
<td>Thermal diffusivity</td>
<td>( \kappa )</td>
<td>10^{-6} m²/s</td>
</tr>
<tr>
<td>Lithosphere temperature drop</td>
<td>( \Delta T )</td>
<td>1400 K</td>
</tr>
<tr>
<td>Viscosity, upper mantle</td>
<td>( \mu_0 )</td>
<td>10^{21} Pa s</td>
</tr>
<tr>
<td>Viscosity, mean mantle</td>
<td>( \mu )</td>
<td>30 ( \mu_0 )</td>
</tr>
<tr>
<td>Viscosity, continent</td>
<td>( \mu_c )</td>
<td>( \mu_0 )</td>
</tr>
<tr>
<td>Mantle depth</td>
<td>( D )</td>
<td>3000 km</td>
</tr>
<tr>
<td>Continent 2-D volume</td>
<td>( V )</td>
<td>40 km \cdot D/3</td>
</tr>
</tbody>
</table>

2.5. Dimensionless Governing Equations

We nondimensionalize length by \( \delta \) and time by \( \delta^2/(4\kappa) \), such that

\[
\frac{du}{dt} = \frac{3B\eta u}{u^3 + (\eta - u)^3} - \frac{2yB}{u(\eta - u)} \left( \frac{du}{dt} \right)^2 \tag{9a}
\]

and

\[
\frac{dr}{dt} = \frac{\kappa s^5}{r^4} - ur \tag{9b}
\]

where

\[
\eta = \frac{D}{\delta}, \quad B = \frac{8\eta\mu}{R_c\mu_0},
\]

\[
C = \frac{16\rho'V^2}{9\eta\Delta T\delta^3 D},
\]

and

\[
\kappa s^5 = \frac{c\rho'gV^3}{4\kappa\mu_c\delta^3} \tag{10}
\]

and we have assumed for simplicity that \( \eta \gg 1 \) in developing (9). The dimensionless parameters represent the aspect ratio between convection cell size and slab thickness \( \eta \), the mantle drag on the slab \( \mathcal{B} \), the continental drag on the plate \( \mathcal{C} \), and the collapse rate of the continent \( \mathcal{K} \).

Using \( R_c \approx 660 \) and typical model properties (see Table 1), then \( \eta \approx 40 \), while \( \mathcal{B}, \mathcal{C}, \) and \( \mathcal{K} \) are all \( O(10) \).

3. Analysis

3.1. Equilibrium States

Apart from the null solution, the steady state solution \( u_0 \) to (9) satisfies

\[
\left( 1 - \nu \right) u_0^{2/3} (3u_0^2 - 3\nu u_0 + \eta^2) - 3Bu_0 = 0 \tag{11}
\]

where \( \nu = C/K^2 \), which, given the typical sizes of \( C \) and \( K \), is a small number. If we assume \( \nu \ll 1 \), then the two steady solutions are simply

\[
u_0 = \frac{1}{2} (\eta + \mathcal{B}) \pm \frac{1}{2} \sqrt{(\eta + \mathcal{B})^2 - \frac{8}{3} \eta^2} \tag{12}
\]

Viable solutions are limited by the conditions that \( u_0 \leq \eta \) and that \( u_0 \) is real; these imply that \( 2/\sqrt{3} - 1 \leq \mathcal{B}/\eta \leq 1/3 \), which, by (10), corresponds to a plausible viscosity ratio range of 13 \( \leq \mu/\mu_0 \leq 28 \). For the upper limit \( \mathcal{B}/\eta = 1/3 \), solutions are
each of the two steady solutions $u_1$ and $u_2$ is unstable while the short-plate solution $u_0 = \eta$ is unstable. For the long-plate solution, we have $u_0 = (2 \pm 1)\eta/3$; i.e., either the plate is at the full possible length or has rolled back to $1/3$ its full length. (For the lower limit, there is only one solution $u_0 = \eta/\sqrt{3}$). The associated velocities $w = 4\kappa u/\delta$ are, for $B/\eta = 1/3$, 6 and 2 cm/yr, for the long- and short-plate solutions, respectively.

Although $\nu = C/\kappa^2$ is small, it influences the steady state solutions, which are found numerically (see Figure 2a). While the range of solutions for $u_0$ do not change, they occur for smaller values of $B$. For $\nu \approx 0.1$, the range of allowable $B$ is $0.1 \leq B/\eta \leq 0.19$, which corresponds to the viscosity ratio range $8 \leq \mu/\mu_0 \leq 16$. Thus, the continental pile exerts enough resistance that steady solutions only exist if the lower mantle viscosity is reduced.

Although the two equilibrium solutions for $u_0$ have significantly different lengths and velocities, the associated widths of the continental pile $r_0 = \kappa u_0^{-1/3}$ have little variation. The ratio of the continental widths for the shortest- and longest-plate states (given by $u_0 = (2 \pm 1)\eta/3$) is simply $3^{1/3} \approx 1.25$. Thus, the continental pile lengths by 25% from one equilibrium state to the other.

### 3.2. Stability

The rollback instability is inferred from the stability of the equilibrium solutions $(u_0, r_0)$ from section 3.1. Substituting infinitesimal perturbations to these solutions $(u, r) = (u_0, r_0) + \epsilon(u_1(t), r_1(t))$, where $\epsilon \ll 1$, into (9), we obtain to $O(\epsilon^1)$:

\[
\frac{du_1}{dt} = \left(1 - \frac{C}{\kappa^2} u_0^{2/3}\right) \frac{3u_0^2 - \eta^2}{3u_0(u_0 - \eta) + \eta^2} u_1 + \frac{2\epsilon u_0^{8/3}}{\kappa^3} r_1
\]

\[
\frac{dr_1}{dt} = -\frac{\kappa}{u_0^{1/3}} u_1 - 5u_0 r_1
\]

Using $(u_1, r_1) \sim e^{st}$ in (13), we infer a quadratic relation for the growth rate $s$ and thus two growth rates for each of the two steady solutions $u_0$. For the case of $\nu = C/\kappa^2 \ll 1$, only the evolution equation for $u_1$ is needed and

\[
s = \frac{3u_0^2 - \eta^2}{3u_0(u_0 - \eta) + \eta^2} \quad (14)
\]

In the case of $B = \eta/3$ and $u_0 = (2 \pm 1)\eta/3$, the growth rates are $s = \pm 2$; i.e., the equilibrium long-plate solution $u_0 = \eta$ is unstable while the short-plate solution $u_0 = \eta/3$ is stable. The maximum growth rate...
The supercontinent slab configuration is unstable, and the slabs retreat to a stable state with shorter plates. The process of rolling back, and the associated in-fill of mass between the two retreating slabs, would then disperse the continent between the slabs.

3.3. Rollback Velocity

The nonlinear evolution equations (9) can be used to infer the rollback velocity \( du/dt \) as the trench retreats from the long- to short-plate states. For the simple case with \( \nu = C/K^2 \ll 1 \) the governing equations are decoupled and \( du/dt \) is only a function of \( u \).

For the general case of \( \nu > 0 \), we assume that \( dr/dt \approx 0 \); i.e., since both terms on the right side of (9b) are very large, they are likely much bigger than their difference \( dr/dt \). In this case, using \( r \approx K \nu^{-1/5} \) in (9a), we obtain a closed and integrable relation for the rollback velocity:

\[
\frac{du}{dt} = F(u) = \frac{u(\eta - u)}{4\gamma B} \left( -1 + \sqrt{1 + \frac{8\gamma B}{\eta - u} \left( 1 - \nu u^2/3 - \frac{3B\nu u}{u^3 + (\eta - u)^3} \right) } \right)
\]

(Figure 3). We also verify the assumption that \( dr/dt \approx 0 \) for cases with \( \nu > 0 \) by comparing (15) to full numerical solutions of (9); see Figure 3b.) The rollback velocity is negative as the system evolves from the long- to short-plate equilibria. In principle, trench advance could occur if the initial plate is longer than in the unstable equilibrium state, but in that case there is no stable state to which it can evolve.) In all cases, the maximum absolute rollback velocity \( |du/dt| \) is comparable to but generally less than the peak plate velocity \( u \) (which agrees with Schellart et al. (2007)) and occurs roughly at the midpoint between the two equilibrium lengths of \( u \) (recall that \( u \) represents both dimensionless plate speed and length). At these velocities, the rollback instability can disperse continental crust at a tectonically feasible rate.

3.4. Rollback Time

The integration of (15) between the long-plate and short-plate equilibrium states gives the net rollback time

\[
t_{rb} = \int_{u_l}^{u_s} \frac{du}{F(u)}
\]

where the \( u_l \) are the long- (\( j = l \)) and short-plate (\( j = s \)) equilibrium solutions. The rollback time appears most sensitive to the continental drag factor \( \nu = C/K^2 \) (Figure 4). Using \( R_c \approx 660 \) and properties from Table 1, the dimensional rollback time is typically 200–400 Myrs, which is commensurate with the age of ocean basins and the period of the Wilson cycle.

4. Summary and Conclusion

Trench migration plays an important role in mantle flow patterns, back-arc deformation and volcanism, and arc/slab morphology in subduction systems [Lallemand et al., 2008; Clark et al., 2008; Long and Silver, 2009; Stegman et al., 2010; Long et al., 2012; Crameri and Tackley, 2014]; we suggest that it may also play a crucial role in the supercontinent cycle. In particular, our simple theory illustrates how a “supercontinent” configuration of subduction zones is naturally unstable to slab rollback and trench retreat and evolves to a stable state of dispersed slabs and continents. This mechanism provides an alternative to continental dispersal via
mantle thermal insulation and induced upwelling [e.g., Gurnis, 1988; Lenardic et al., 2011; Yoshida, 2013], which is problematic if the mantle Urey number is small [Korenaga, 2008; Jaupart et al., 2007]. In contrast, our proposed rollback instability is purely mechanical and independent of heating mode. Moreover, the slab rollback velocity implied by the model is comparable to typical tectonic plate velocities; hence the rollback time (to go from the unstable supercontinent state to the stable dispersed-continent state) is comparable to the age of ocean basins and the Wilson cycle period. The model is idealized in that it is 2-D, neglects possible effects of complex rheology and strength in the lithosphere (leading to self-weakening and/or strong continental lithosphere), and does not account for the agglomeration cycle, which we assume is inevitably driven by convergence over convective downwellings (although whether by “extroversion” or “introversion” remains debated [e.g., Murphy et al., 2009]). Nevertheless, our simple model provides feasible predictions for supercontinent dispersal and a framework for further, more sophisticated investigations.

References


Wilson, J. (1966), Did the Atlantic close and then re-open?, *Nature*, **211**, 676–681.


