4.6 Fluid Flow in the Deep Crust

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4.6.1 Introduction

The heating and burial of rock masses during mountain building drives chemical reactions that liberate volatile fluid species (Figure 1). These volatiles, including H₂O, CO₂, and CH₄, are much less dense and viscous than the surrounding rock and will, therefore, have a strong tendency to migrate along grain boundaries or fractures through the Earth’s crust. Fluids released in the deep crust interact geochemically with their surroundings (Rye et al., 1976) as they ascend to shallow levels where they invade hydrothermal and groundwater systems and, ultimately, interact with the hydrosphere and atmosphere. This flux of fluid from actively metamorphosing mountain belts to the surface is a major contributor to planetary volatile cycling and is estimated to be currently in excess of ~10¹⁷ kg per million years (based on Kerrick and Caldeira, 1998; Wallmann, 2001a,b).

The deep crust is composed largely of metamorphic rock (Rudnick and Fountain, 1995; Wedepohl, 1995). Fluids and magmas are the primary agents of chemical mass transport through the deep crust; fluid flow dominates at temperatures <600 °C and can be important at much higher temperatures as well – even in the granulite facies. As a consequence, an understanding of the fundamental controls exerted by metamorphic fluids on mass and heat transfer, mineral reactions, and rock rheology is critical for determining the geochemical and petrological evolution of the crust. Moreover, metamorphic fluids impact directly many problems of societal relevance, including ore deposit formation, global release of greenhouse gases, seismic hazards, and arc magma genesis and the associated volcanic hazards.

In this chapter, basic fluid flow, mass transfer, and reaction concepts will be examined first. This discussion is followed by
4.6.3 Devolatilization

The fact that rocks lose volatiles during metamorphic heating is a fundamental tenet of petrology (Fyfe et al., 1978; Shaw, 1956). Devolatilization is a ubiquitous source of fluid during mountain building, although other sources, including degassing magmas and the mantle, can also play important roles. Pseudosection phase diagrams (Connolly, 1990; de Capitani and Petrakakis, 2010; Powell et al., 1998) for representative aluminous pelite, hydrothermally altered mafic rock (spillite), and ultramafic rock are shown in Figure 2 to illustrate rock water contents as a function of pressure and temperature (P–T) conditions. Of course, different bulk compositions will yield different phase relations, but the general patterns depicted in the figures will be robust.

The diagrams illustrating the wt% water in solids (right panels in Figure 2) show the substantial water loss expected for prograde metamorphism. Metapelitic rocks, for example, will typically lose 2–4 wt% H₂O from low to high grade (Figure 2(a)). This general prediction corresponds well with field relations. Pattison (2006), for example, documented ~2.9 wt% volatile loss from metapelitic rocks between 550 and 625 °C (~4.5 mol l⁻¹); numerous similar examples can be found in the literature (e.g., Fyfe et al., 1978). The water loss corresponds to reactions that destroy hydrous phases, like muscovite, chlorite, and lawsonite, to produce less hydrous or nominally anhydrous ones, such as garnet, aluminosilicates, and pyroxene. The greenschist–amphibolite and blueschist–eclogite facies transitions correspond in a general way to the disappearance of chlorite (Figure 2(a)), although the reader is cautioned that the stability of chlorite and other phases is dependent on the bulk composition of the rock. As is well known, water will be retained to greater depths along subduction zone geotherms, as opposed to the P–T paths characteristic of continental collisions (Figure 2(a); Chapters 4.19 and 4.20).

It is generally held that most dehydration accompanies prograde heating, but if reaction dP/dT slopes are shallow relative to the P–T path, then some dehydration can even occur during cooling and exhumation. For example, the schematic collisional path in Figure 2(a) passes from the 3 wt% to the 2.5 wt% field during exhumation. Vry et al. (2009) provide evidence for volatile loss during exhumation of the Alpine Schist, New Zealand.

The diagram for metamorphosed spillite indicates loss of 2–4 wt% water during heating to amphibolite facies conditions (Figure 2(b)). By contrast, substantial water is retained in the high-pressure, low-temperature part of the blueschist facies to pressures of 2 GPa and beyond (Chapters 4.19 and 4.20). Steep drops in water content down to 2–3 wt% in the eclogite facies and the higher-T part of the blueschist facies are due largely to lawsonite breakdown.

The water content contours for an example of partially serpenitized harzburgite differ substantially from the other rock types (Figure 2(c)). Here, even larger amounts of water are lost (up to ~10 wt%), and the major episodes of water loss take place over relatively narrow temperature intervals. The first of these (at lower T) corresponds to the destruction of brucite and some of the antigorite (a serpentine-group mineral); it involves loss of ~2 wt% H₂O in the greenschist and blueschist facies. The second occurs at higher T in the...
Figure 2 (Continued)
amphibolite or eclogite facies, corresponds to the destruction of antigorite, and releases 5–6 wt% H₂O over a T interval of only ~10–20 °C. The reactions take place over narrow temperature intervals, as there is relatively little solid solution in the phases involved owing to the bulk composition, which is dominated by MgO, SiO₂, and H₂O. The intervals would be somewhat wider if iron–magnesium solid solution in antigorite and brucite could be accounted for, but the effects are expected to be minor, as these phases are dominated by magnesium (iron–magnesium–aluminum solution is accounted for in the other solids). The release of large amounts of water over small temperature ranges has important implications for rock rheology, as discussed further in the succeeding text.

The diagrams depict water loss due to dehydration, but other volatiles, particularly CO₂, are also critical components of metamorphic fluids. Devolatilization reaction progress in C-bearing systems is a strong function of fluid composition and reaction history; thus, it is not possible to depict simply on diagrams like Figure 2. Field studies, however, document the large quantities of volatiles that are lost. For example, Ferry (1992) and Léger and Ferry (1993) studied infiltration-driven devolatilization of impure carbonate rocks intercalated with metaclastic rocks in the Waits River Formation, Vermont, United States, which underwent broadly Barrovian-style metamorphism during the Acadian orogeny. Ague (2003) studied similar rocks in the Wepawaug Schist, Connecticut, United States, and highly reacted zones along flow conduits.

In both field settings, volatile loss was extensive; on average, ~15 kg volatiles were lost from typical amphibolite facies rocks (diopside zone) relative to 100 kg of low-grade protolith (Figure 3). More than 95% of this volatile mass was CO₂. The low-grade protolith rocks contain considerable calcite, ankerite, albite, muscovite, and quartz. These combined to yield a rich spectrum of devolatilization reactions that operated during heating and produced minerals like biotite, calcic amphibole, and diopside with increasing grade. Volatile losses were even larger – about 25 wt% – in highly altered, amphibolite facies calc-silicate rocks situated along fluid conduits, such as lithologic contacts and quartz veins (Figure 3; Ague, 2003). As metacarbonate rocks comprise 20–50% of the western part of the Waits River Formation, 50–80% of the eastern part, and about 10% of the Wepawaug Schist, the production of CO₂ clearly played a significant role in the overall deep-crustal (25–35 km) volatile budget.

Other kinds of devolatilization systematics are, of course, possible. Many rocks will contain hydrous minerals and carbonate minerals, such that substantial amounts of both CO₂ and H₂O are liberated from the same lithology. Ferry (1994a,b) found that carbonate-bearing metasandstones and

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**Figure 3** Loss of CO₂ and H₂O from impure carbonate rocks during regional metamorphism; Waits River Formation, Vermont (Ferry, 1992; Léger and Ferry, 1993) and the Wepawaug Schist, Connecticut (Ague, 2003). Prograde reaction progress increases to the right. Kilograms lost relative to 100 kg of average low-grade (Ankerite–Albite zone) precursors. Mean values shown, together with their 1σ standard errors (shaded fields around lines). CO₂ comprises over 95% of the lost mass. Calculations for Wepawaug are described in Ague (2003). Calculations for the Waits River used the aluminum geochemical reference frame of Ferry (1992) and Léger and Ferry (1993); loss on ignition as a proxy for volatile content; and eqns [21.99]–[21.100] in Philpotts and Ague (2009).

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(b) hydrothermally altered basalt, and (c) ultramafic rock. Facies boundaries after Spear FS (1993) *Metamorphic Phase Equilibria and Pressure–Temperature–Time Paths*. Washington, DC: Mineralogical Society of America and Philpotts AR and Ague JJ (2009) *Principles of Igneous and Metamorphic Petrology*, 2nd edn. Cambridge: Cambridge University Press. Calculated using Theria–Domino software and thermodynamic dataset tcdb55c2d (de Capitani and Petrakakis, 2010); dataset based on Holland and Powell (1998) and includes recent updates. Tick marks on P-axis are 0.05 GPa. (a) Aluminous metapelite TNG20 (Nagel et al., 2002). Note schematic subduction zone and collisional P–T paths (yellow dashed lines) on wt% water diagram. KNaCaFMSASH system. Provisional ideal mixing model used for glaucophane–ferroglaucophane solid solution. All mineral assemblages coexist with water and quartz, except those marked –q that lack quartz. Beginning of water-saturated partial melting denoted with dashed red line. (b) Hydrothermally altered mafic rock (spilitite), sample SF-2100, California. Rock composition reproduced from Coleman RG and Lee DE (1963) Glaucophane-bearing metamorphic rock types of the Cazadero area, California. *Journal of Petrology* 4: 260–301. KNaCaFMSASH system. Provisional ideal mixing models used for sodic amphibole (glaucophane–ferroglaucophane) and calcic amphibole (tremolite–ferrotremolite–paragastite) solid solutions. All assemblages coexist with water. Beginning of water-saturated partial melting denoted with thin dashed red line, but melt phase relations not shown due to current uncertainties in mineral–melt equilibria for metabasaltic systems. (c) Partially serpentinitized harzburgite, sample 65-R-10, California. Rock composition reproduced from Himmelberg GR and Coleman RG (1968) Chemistry of primary minerals and rocks from the Red Mountain-Del Puerto ultramafic mass, California. *United States Geological Survey Professional Paper 600-C, C18–C26*. FMSASH system; small amounts of Ca and Fe⁴⁺ not considered. Phase abbreviations for all plots: atg, antigorite; b, biotite; br, brucite; ca, calcic amphibole; cd, cordierite; ch, chlorite; cp, calcic clinopyroxene; ctd, chloritoid; cz, clinozoisite; g, garnet; k, kyanite; law, lawsonite; m, melt; mu, muscovite (contains substantial phengite component at high pressures); na, Na amphibole; np, Na pyroxene; opx, orthopyroxene; pg, paragonite; pl, plagioclase; q, quartz; sil, sillimanite; st, staurolite; tlc, talc; w, water.
metapelites of the Waits River Formation lost, on average, 4.25 mol total fluid (several wt% CO₂ + H₂O) per liter rock over the comparatively small temperature interval of 475–550°C. Relatively pure marbles and quartzites will generate little fluid during heating, but these rock types are not dominant in most metasedimentary sequences (although there are of course exceptions, such as the thick marbles of Naxos, Greece). Intrusive and extrusive igneous rocks may have a wide range of volatile contents, depending on bulk composition, crystallization history, and the extent of postmagmatic hydrothermal alteration. Strongly altered rocks, like spillites, will act as volatile sources during heating, whereas less hydrous igneous protoliths may act as fluid sinks, particularly if infiltration and the accompanying hydration and/or carbonation reactions occur at low metamorphic grades. Hydration and carbonation reactions typically produce increases in solid volume. Traditionally, this has been thought to close off porosity and, thus, limit infiltration. However, recent work suggests that it is possible that volume production by such reactions could generate enough stress to fracture rocks, creating new pathways for fluid flow (Jamtveit et al., 2008; Kelemen and Matter, 2008).

4.6.4 Porous Media and Fracture Flow

Fluid flow through rocks is commonly referred to as being pervasive or channelized, although some overlap exists in the definitions of these terms. Fluid migration around individual mineral grains through an interconnected porosity is known as pervasive or porous media flow (Figure 4). Channelized or focused flow implies preferential fluid motion in one or more high-permeability conduits (Figure 5). These include highly permeable layers, lithologic contacts, fracture sets, or individual fractures. Note that flow in a permeable layer could still be pervasive at the grain scale within the layer, whereas flow in a fracture is much more strongly localized to the open space between the crack walls. Some metamorphic systems involve both channelized and pervasive flow components (e.g., Oliver, 1996; Rumble et al., 1991).

Figure 4  Schematic representation of metamorphic porphyroblasts and matrix illustrating concept of pervasive, grain-scale flow. Flow paths around grains denoted by black arrows.

Figure 5  Examples of channelized flow.

4.6.4.1 Pervasive Flow and Darcy’s Law

Pervasive fluid flow through a porous, permeable medium is described by Darcy’s law, written here for three dimensions (e.g., Bear, 1972):

\[
\vec{q}_D = \left( \frac{\partial P}{\partial x}, \frac{\partial P}{\partial y}, \frac{\partial P}{\partial z} \right) = -\frac{k}{\mu} \left( \frac{\partial Z}{\partial x}, \frac{\partial Z}{\partial y}, \frac{\partial Z}{\partial z} \right) + \rho_f g \nabla Z
\]

in which \( x, y, \) and \( z \) are Cartesian spatial coordinates; \( \vec{q}_D \) is the fluid flux vector or Darcy flux (\( q_x, q_y, \) and \( q_z \) are the components of the flux in the \( x, y, \) and \( z \) directions, respectively); \( k \) is the intrinsic permeability tensor; \( \mu \) is the dynamic viscosity of the fluid; \( P \) is fluid pressure; \( \rho_f \) is fluid density; \( g \) is the acceleration of gravity expressed as a constant (9.81 m s⁻²); and \( Z \) is a vertical reference coordinate axis that increases upward (Table 1). Darcy’s law is valid only when the flow is laminar, not turbulent (Bear, 1972, pp. 125–129). Note that fluid flux is a vector, having both magnitude and direction. Clearly, the flux is increased by increasing permeability, increasing fluid pressure gradients, and/or decreasing the fluid viscosity. These key geologic variables are examined in the following paragraphs.
Thus, estimates of syn-metamorphic porosity of Connolly (1997) are volume rock (volume rock saturated porous medium is the fluid volume in pores per unit volume). For example, if $q = 10^{-3} \text{m}^3 \text{m}^{-2} \text{s}^{-1}$ and $\phi = 10^{-3}$, then the pore velocity, $v_{p}$, is $1 \text{ m year}^{-1}$. If the total porosity includes some dead end pores that are not interconnected and do not transmit fluid, then $\phi$ in eqn [2] must be reduced by multiplying it by the fraction of interconnected pore space.

Porosity evolves as a result of deformation and fluid–rock reactions. Four general pathways of porosity evolution are commonly recognized. First, deformation can collapse porosity and drive fluids out or produce cracking at the grain scale or larger to create porosity. The low-porosity values estimated by Bickle and Baker (1990) for nearly pure marbles may reflect the relative ease with which calcite can deform plastically (e.g., Rutter, 1995) and choke off porosity. Second, increases in fluid pressure will tend to expand pore spaces and increase porosity, whereas decreases in pressure will do the opposite (Walder and Nut, 1984). Third, the mineral products of prograde reaction are typically denser and occupy less volume than reactants, so increases in porosity may accompany fluid infiltration and devolatilization if fluid pressure is sufficient to keep the pore space from collapsing (e.g., Ague et al., 1998; Balashov and Yardley, 1998; Rumble and Spear, 1983; Zhang et al., 2000). The coupled metamorphic– rheological models of Connolly (1997) suggest that devolatilization reactions generate pulses of fluid that travel upward in the form of porosity waves, leaving trails of interconnected pore space in their wake (Section 4.6.4.7). Finally, infiltrating metasomatic fluids will destroy porosity if they precipitate new minerals in the pore spaces or create porosity if they dissolve existing minerals (Balashov and Yardley, 1998; Bolton et al., 1999). In addition to the four processes mentioned earlier, Nakamura and Watson (2001) have shown experimentally that interfacial energy-driven infiltration of water or NaCl-bearing aqueous solution into quartzite can create high-porosity zones that propagate through rock much like traveling waves. Nakamura and Watson (2001) suggest that this mechanism may contribute significantly to fluid fluxes in high-grade metamorphism.

### Fluid Pressure Gradients

Fluid motion occurs in a direction of decreasing pressure. In Darcy’s law, the driving pressure gradient is given by $(\nabla P_{f} + \rho_{f} g \nabla Z)$. The $\rho_{f} g \nabla Z$ term is necessitated by gravity. Pressure increases downward in a column of motionless fluid according to the hydrostatic gradient ($-\rho_{f} g$), yet there is no flow. To drive flow upward, the total pressure gradient must exceed the hydrostatic gradient. For convenience, the $z$-axis of the coordinate system is commonly oriented vertically so that it coincides exactly with the vertical reference $Z$-axis. Then, $\partial Z/\partial x$ and $\partial Z/\partial y$ are 0, and $\partial Z/\partial z$ is 1. For example, the net pressure gradient driving the vertical component of flow would be given by the difference between the total pressure gradient, $\partial P_{f}/\partial z$, and $-\rho_{f} g$, thus yielding $\partial P_{f}/\partial z - (-\rho_{f} g)$ or, equivalently, $\partial P_{f}/\partial z + \rho_{f} g$.

Brittle deformation involves fracturing on the scale of individual mineral grains or larger, whereas ductile (plastic) deformation occurs without fracturing (e.g., Passchier and Trouw, 1996). In the shallow crust, rocks are in the brittle regime, have substantial strength, and can support open pore networks over kilometer-scale distances. Fluid pressure gradients are close to the hydrostatic gradient, and free convection cells may develop if permeability and thermal gradients are large enough, as is

<table>
<thead>
<tr>
<th>Symbol</th>
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<tr>
<td>$x$, $y$, $z$</td>
<td>Subscripts denoting $x$-, $y$-, $z$-axes</td>
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<tr>
<td>$Z$</td>
<td>Vertical reference coordinate</td>
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<tr>
<td>$x'$</td>
<td>Coordinate which is parallel to, and increases in, the direction of flow</td>
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<tr>
<td>$2b$</td>
<td>Distance between fracture walls (m)</td>
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<td>$B$</td>
<td>Thermal Peclet number</td>
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<tr>
<td>$C_{f}$</td>
<td>Heat capacity of fluid (J kg$^{-1}$ K$^{-1}$)</td>
</tr>
<tr>
<td>$f_{m}$</td>
<td>Mass fluid released per unit mass solid (kg (fluid) kg$^{-1}$ (solid))</td>
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<tr>
<td>$f_{mv}$</td>
<td>Mass fluid released per unit volume rock (kg (fluid) m$^{-3}$ (rock))</td>
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<tr>
<td>$g$</td>
<td>Acceleration of gravity (m s$^{-2}$)</td>
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<td>$K_{12}$</td>
<td>Thermal conductivity of rock (J m$^{-1}$ s$^{-1}$ K$^{-1}$)</td>
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<tr>
<td>$k$</td>
<td>Permeability tensor (m$^2$)</td>
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<tr>
<td>$k$</td>
<td>Permeability (constant) (m$^2$)</td>
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<tr>
<td>$k_{i}$</td>
<td>Permeability due to fractures (m$^2$)</td>
</tr>
<tr>
<td>$L_{c}$</td>
<td>Length of crustal column (m)</td>
</tr>
<tr>
<td>$n_{f}$</td>
<td>Frequency of fractures (fractures m$^{-1}$)</td>
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<td>$P$</td>
<td>Pressure</td>
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<td>$P_{f}$</td>
<td>Fluid pressure</td>
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<td>$q_{D}$</td>
<td>Darcy flux vector (m$^3$ m$^{-2}$ s$^{-1}$)</td>
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<td>$q_{f}$</td>
<td>Fluid flux through fractured rock (m$^3$ m$^{-2}$ s$^{-1}$)</td>
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<td>Time-integrated fluid flux (m$^3$ m$^{-2}$ s)</td>
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<td>$t$</td>
<td>Time (s)</td>
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<td>Total time of fluid–rock interaction (s)</td>
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<td>$v$</td>
<td>Pore velocity vector (m s$^{-1}$)</td>
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<td>Dynamic viscosity of fluid (Pa s)</td>
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<td>$\rho_{f}$</td>
<td>Fluid density (kg m$^{-3}$)</td>
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<td>$\rho_{i}$</td>
<td>Rock density (kg m$^{-3}$)</td>
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<tr>
<td>$\rho_{s}$</td>
<td>Solid density (kg m$^{-3}$)</td>
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<tr>
<td>$\phi$</td>
<td>Porosity (m$^3$ (fluid) m$^{-3}$ (rock))</td>
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<tr>
<td>$\omega$</td>
<td>Constant for porosity–permeability law (m$^2$)</td>
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often the case around cooling intrusions (Norton and Dutrow, 2001; Norton and Knight, 1977). Furthermore, groundwater can circulate down into sedimentary basins to depths of several kilometers by gravity-driven (or topography-driven) flow involving fluid input into high-elevation parts of foreland basins, subhorizontal flow for tens or even hundreds of kilometers, and discharge into lower-elevation areas (Garven and Freeze, 1984a, 1984b).

The transition between hydrostatic and deeper regimes is thought to occur at around 10 km (e.g., Manning and Ingebritsen, 1999), but is not precisely constrained and may be considerably deeper. At deeper levels, where plastic deformation becomes more important, rocks are considerably weaker and tend to collapse around fluid-filled pores, producing larger pressure gradients that may approach lithostatic (dP/dz = −ρg; ρi is rock density). Thus, for vertical, upward flow under the lithostatic gradient, the pressure gradient term in Darcy’s law is the difference between the lithostatic and hydrostatic gradients (−ρg + ρi g ≈ −1.7 × 104 to −2.0 × 104 Pa m−1 ≈ 0.17 to −0.2 bar m−1). In general, deep-crustal fluid pressure regimes that drive flow are thought to be closer to lithostatic than hydrostatic (e.g., Hanson, 1997), but much uncertainty remains. For example, the subhorizontal flow constrained by nearly flat-lying lithologic layering inferred on petrologic grounds for regional metamorphism in northern New England by Ferry (1992, 1994a) could have been driven by very small gradients – even smaller than the hydrostat (<105 Pa m−1).

### 4.6.4.4 Permeability

The intrinsic permeability is a property of the porous medium only and is a quantitative measure of how readily a fluid can flow through the medium. Permeability varies over a remarkable 16 orders of magnitude in the Earth’s crust, from values as high as 10−2 m2 in gravels to 10−23 m2 in some shales and crystalline igneous and metamorphic rocks (e.g., Brace, 1980; Connolly, 1997; Freeze and Cherry, 1979; Manning and Ingebritsen, 1999). In the general case, k is a second-rank tensor because permeability varies with direction. Metamorphic foliations defined by inequidimensional minerals, particularly sheet silicates, are a primary source of anisotropy (e.g., Zhang et al., 2001). The measurements of Huenges et al. (1997) reveal mean permeability parallel to foliation as much as ∼10 times greater than perpendicular to it, consistent with field-based studies that suggest fluid fluxes are greatest parallel to layering and foliation (e.g., Baker, 1990; Cartwright et al., 1995; Ferry, 1987, 1994a,b; Ganor et al., 1989; Oliver et al., 1990; Rumble and Spear, 1983; Rye et al., 1976; Williams et al., 1996). Oriented fracture sets are another source of anisotropy. If, on the other hand, the medium is isotropic and can transmit fluid equally well in all directions, then k reduces to a constant (k). Permeability also varies from one layer to the next and even within individual layers, regardless of the degree of anisotropy, producing permeability contrasts that can exceed two orders of magnitude (Baumgartner and Ferry, 1991; Baumgartner et al., 1997; Oliver, 1996). Comparisons of inferred metamorphic fluid fluxes suggest that metablastic rocks are often more permeable than metasammites or very pure calcite marbles (e.g., Chamberlain and Conrad, 1991; Oliver et al., 1998; Rye et al., 1976; Skelton et al., 1995).

Following the approach of Baumgartner and Ferry (1991), Manning and Ingebritsen (1999) estimated a mean k of 10−18.5±1 m2 for rocks deeper than ~12 km undergoing active metamorphism and combined this result with permeability data for shallower geothermal systems to yield the depth–permeability relation: log k ≈ −3.2 log(depth in km) − 14. Permeability likely exceeds these predicted values during transient events that increase porosity and permeability, such as earthquake faulting, and falls below these values in quiescent rocks undergoing little metamorphism or deformation (Ingebritsen and Manning, 2010). Although considerable uncertainty remains regarding crustal depth–permeability relationships (Connolly, 2010), available estimates strongly suggest that significant permeability is possible even at the base of the continental crust during orogenesis.

In general, permeability increases as the amount of interconnected pore space increases, resulting in strong coupling between porosity and permeability. Thus, because porosity is time-dependent, permeability is as well. A number of porosity–permeability relationships, such as the Kozeny–Carman equation, have been proposed; these commonly include a strong (often cubic) dependence of permeability on porosity (e.g., Bear, 1972, p. 166; Bickle and Baker, 1990; Bolton et al., 1999; David et al., 1994; Walder and Nur, 1984; Wong and Zhu, 1999; and references therein). For example, Connolly (1997) described deep-crustal permeability using k = ωq3 in which the constant ω = 10−13 m2. While calculated porosity–permeability relationships are still subject to major uncertainties of order of magnitude scale or larger, it is clear that porosity–permeability feedbacks can control spatial patterns of flow. For example, increases in porosity due to infiltration and devolatilization reaction can increase permeability, causing more flow to focus into the reacting area (e.g., Balashov and Yardley, 1998; Spiegelman and Kelemen, 2003), whereas precipitation of minerals that occlude the porosity can decrease permeability and divert flow away (e.g., Lyubetskaya and Ague, 2009).

### 4.6.4.5 Dynamic Viscosity

The dynamic viscosity is the viscosity of a moving fluid; it depends on T, P, and fluid composition. Values for pure H2O, CO2, and, by extension, H2O–CO2 mixtures are similar and vary relatively little compared to properties like porosity and permeability; a representative value for the middle and lower crust is ~1.5 × 10−4 Pa s (see Walther and Orville, 1982). However, the effects on viscosities of solute species, as well as very high pressures (1–2 GPa), remain to be fully explored.

### 4.6.4.6 Crack Flow

The deformational behavior of rocks, whether brittle or ductile, depends mainly on temperature, fluid pressure, rock pressure, mineralogy, grain size, and strain rate. Temperature is one of the main controls on deformation behavior. For example, for slow strain rates, common minerals, like quartz, are brittle at T <=~300 °C, but ductile deformation involving dislocation glide and creep becomes increasingly important at higher T. The transition from dominantly brittle to dominantly ductile behavior is thought to occur at depths corresponding to temperatures of ~300 °C – usually around ~15 km for typical
crustal geotherms (e.g., Scholz, 1990; Sibson, 1983; Yeats et al., 1997). These depths are consistent with measured and inferred near-hydrostatic fluid pressure gradients in much of the shallow crust.

Nonetheless, brittle behavior is not restricted to shallow levels. If the fluid pressure exceeds the sum of the tensile strength of the rock and the least principal stress, then hydrofracturing, transient fluid release, and associated drops in fluid pressure will occur (e.g., Etheridge, 1983; Hubbert and Willis, 1957; Yardley, 1986). The maximum tensile strength of most rocks is only ∼0.01 GPa (∼100 bars), so even modest fluid overpressures will cause hydrofracturing. Elevated pore fluid pressures generated by metamorphic devolatilization reactions (e.g., Ague et al., 1998), as well as by deformation and collapse of pore space (e.g., Cox, 2007; Sibson, 1992; Sibson et al., 1975; Walder and Nur, 1984; Wong et al., 1997), can lead to rock weakening and hydrofracture. With time, the porosity and permeability created by a hydrofracturing event are reduced as cracks are sealed and pores collapse. If permeability reaches low enough levels (<10⁻²⁰ m²), then fluid pressure can once again build up and ultimately produce another hydrofracturing event. The episodes of fracturing and healing preserved in veins attest to this cyclic behavior (Fisher and Brantley, 1992; Kirschner et al., 1993; Oliver and Bons, 2001; Ramsay, 1980; Rye and Bradbury, 1988). Oxygen isotope disequilibrium suggests transient timescales of fluid-rock interaction as short as 10⁴–10⁵ years in and around some veins (Section 4.6.9.7; Palin, 1992; van Haren et al., 1996; Young and Rumble, 1993). At very shallow crustal levels, hydrofracturing may be less common if relatively high rock permeabilities prevent fluid pressures from building up.

Rocks that are ductile at low strain rates can undergo brittle deformation at larger strain rates. For example, earthquakes release massive amounts of energy in seconds or minutes during fault slippage and are capable of producing regionally extensive brittle deformation. Data from several recent, damaging earthquakes, including the Northridge and Loma Prieta events in California and the Kobe event in Japan, demonstrate that rupture and brittle deformation occur well below 10–13 km (e.g., Davis and Namson, 1994; Lees and Lindley, 1994; Priestley et al., 2008; Zhao et al., 1996). For the Northridge event, the main shock occurred at 17–18 km, and some aftershocks extended to ∼25 km. In fact, from April 1980 to February 1994, nearly 1100 seismic events were recorded in the 20–35 km depth range in the Los Angeles, California area alone (Ague, 1995). If rapid devolatilization and hydrofracturing occur within seismically active areas, then the rock failure may trigger earthquakes that recur on human timescales (e.g., Ague et al., 1998). The fluid-filled earthquake hypocenters that have been inferred on the basis of seismic evidence for both the Loma Prieta (Lees and Lindley, 1994) and Kobe (Zhao et al., 1996) events strongly suggest links between the presence of fluids and seismicity.

The evidence mentioned earlier establishes that fracturing and seismic behavior can extend well into the mid to lower crust. Veins preserve a valuable record of this brittle deformation; they are fractures into which mineral mass has been deposited. The most common vein-forming minerals are quartz, calcite, and the feldspars, but a huge variety of other minerals are also observed. Fractures tend to focus flow because they are zones of elevated permeability. Fracture flow is commonly approximated using the well-known expression from fluid mechanics for laminar flow between two parallel plates (e.g., White, 1979). For a set of parallel fractures, the flux is approximated by (e.g., Norton and Knapp, 1977)

\[
q_f = \frac{(2b)^3n_b}{12m} \left( \frac{dP_t}{dx} + \rho \frac{dZ}{dx} \right)
\]

in which \(q_f\) is the fluid flux through the fractures in the rock mass, the coordinate \(x\) is parallel to, and increases in, the direction of flow, \(2b\) is the distance between the fracture walls (or crack aperture), and \(n_b\) is the frequency of the fractures.

Equation [3] has been shown experimentally to be applicable to real fractures, even those with rough walls and many points of contact (asperities), if \(2b\) is taken as the average crack aperture. By comparison with eqn [1], it is clear that the \((2b)^3n_b/12\) grouping is directly analogous to the permeability in Darcy’s law. Consequently, the fracture permeability, \(k_f\), of a rock mass can be estimated if the average number and aperture of fractures are known (e.g., Norton and Knapp, 1977):

\[
k_f = \frac{(2b)^3n_b}{12}
\]

Metamorphic fracture apertures range from the micrometer scales (Etheridge et al., 1984; Ramsay, 1980) to millimeter or centimeter scales (Ague, 1995).

Even small amounts of fracturing can affect markedly the permeability. If an unfractured rock with low permeability, say \(10^{-23} \text{m}^2\), is deformed to produce, on average, just one \(10^{-5} \text{m}\) aperture fracture per meter of rock \((n_b = 10^{-5} \text{m}^{-1})\), then eqn [4] gives \(k_f \approx 8 \times 10^{-17} \text{m}^2\) — over seven orders of magnitude greater than \(10^{-23} \text{m}^2\). The permeability systematics of crystalline rocks suggest a scale dependence; laboratory measurements made on unfractured rock cores generally yield the smallest values, whereas regional field tests indicate the largest (Brace, 1984). At least some of this discrepancy is probably due to natural fractures that increase considerably the permeability of the field test sites (Manning and Ingebritsen, 1999).

### 4.6.4.7 Porosity Waves

Transient relationships between porosity, permeability, and fluid flow are well illustrated by the concept of porosity waves. Solitary waves of porosity were independently predicted to form in fluid-saturated, compacting porous media by Scott and Stevenson (1984) and Richter and McKenzie (1984). Connolly and coworkers extended the theory to dewatering metamorphic systems (e.g., Connolly, 1997; Connolly and Podladchikov, 1998). Periodic wave behavior is also predicted under appropriate geologic circumstances.

Consider a layer undergoing devolatilization in low-permeability rock. As most devolatilization reactions will decrease solid volume, the porosity and, thus, permeability in the reacting zone will tend to increase. As reviewed by Connolly (2010), this will lead to elevated pressures near the top of the reacting zone and diminished pressures near the base. Given the low strength of rocks, the lower-pressure zone at the base will tend to compact and reduce porosity. Fluids in the upper part, by contrast, will be under elevated pressures and be squeezed upward via dilational deformation of the rock matrix. This coupled
expansion and collapse is predicted to produce a zone of elevated porosity that migrates upward and that can ultimately detach itself from the region undergoing active dewatering. In multiple dimensions, such instabilities are predicted to take elongated, tubelike forms (Connolly and Podladchikov, 2007).

Solitary porosity wave behavior has been experimentally verified for flow through a single nonporous conduit (Olson and Christensen, 1986; Scott et al., 1986). Bouihol et al. (2011) presented field evidence for porosity waves that channelize melt. However, to the author’s knowledge, fluid (as opposed to melt) flow by porosity waves has not been verified for a deformable porous medium either by experiments or by field observations of metamorphic rocks, although some tantalizing field relations have been observed (e.g., John et al., 2012; Podladchikov et al., 2009). Melt formation, segregation, and ascent can involve very large changes in porosity (e.g., Aharonov et al., 1995), but fluid flow need not. As a consequence, the geological fingerprint of porosity wave fluid transport recorded in rocks may be very cryptic. Nonetheless, the more general processes of porosity collapse and compaction undoubtedly play important roles during devolatilization. A major challenge going forward is to assess the nature and extent of fluid propagation by porosity waves in the lithosphere.

4.6.5 Overview of Fluid Chemistry

Metamorphic fluids are chemically diverse and are able to transport molecular species, like H$_2$O, CO$_2$, CH$_4$, and H$_2$S, and solutes, including H$_4$SiO$_4$/C$_{14}$, Na$^+$, NaCl$^-$, and many others (Figure 6). This section provides a brief review of some common fluid constituents.
Deep-crustal H2O is released mostly by prograde devolatilization of sheet silicates and amphiboles and, in some cases, by degassing magmas, whereas CO2 is released mostly by devolatilization of carbonate minerals. Because H2O and CO2 are such fundamental constituents of crustal fluids, considerable attention has been focused on their physicochemical properties. Thermodynamic treatment is complicated because both pure H2O and pure CO2 deviate strongly from ideal gas behavior and because mixing of H2O and CO2 is also nonideal (e.g., Aranovich and Newton, 1999; Blencoe et al., 1999; Ferry and Baumgartner, 1987; Kerrick and Jacobs, 1981; Schmidt and Bodnar, 2000; Shi and Saxena, 1992). The fugacity and activity coefficient expressions of Kerrick and Jacobs (1981) for pure H2O, pure CO2, and H2O–CO2 mixtures have been widely used and are accurate for P ≤ ~1 GPa. Similar results for pure H2O and pure CO2 are obtained using Haar et al. (1984) and Madler and Berman (1991), respectively. Expressions valid for pure species to pressures well in excess of 1 GPa include those of Holland and Powell (1991, 1998), Shi and Saxena (1992), and Sterner and Pitzer (1994). Aranovich and Newton (1999) provide activity–composition relations for H2O–CO2 mixtures valid between ~600–1000 °C and 0.6–1.4 GPa.

H2O and CO2 are extremely important, but deep-crustal fluids contain many other constituents. For example, at low enough oxygen fugacities in the presence of reactive graphite, CH4 can be significant (e.g., French, 1966; Skippen and Marshall, 1991; Connolly, 1995; Figure 6(a)). Furthermore, progressive heating promotes desulfitation of pyrite to produce pyrrhotite and liberate S (e.g., Carpenter, 1974; Mohr and Newton, 1983). Thermodynamic treatments of geologically important species, including CH4, CO, H2, S2, H2S, and COS, can be found in, for example, Holland and Powell (2003), Jacobs and Kerrick (1981) and Shi and Saxena (1992).

Rock-forming and ore-forming metals are key components of aqueous, chloride-bearing metamorphic fluids. Salinity varies from near zero to as much as several molal in typical metamorphic environments (e.g., Crawford and Hollister, 1986; Hollister and Crawford, 1981; Roedder, 1984; Smith and Yardley, 1999; Yardley, 1997) and can reach extreme levels in granulites (Crawford and Hollister, 1986; Markl et al., 1998). Standard state thermodynamic properties for many aqueous species of interest can be calculated to ~1000 °C and ~0.5 GPa using the internally consistent methods and data sets of Pokrovskii and Helgeson (1995), Shock et al. (1997), and Sverjensky et al. (1997). These data have also been extrapolated to somewhat higher pressures with reasonable results (e.g., Dipple and Ferry, 1992a). Holland and Powell (1998) advanced an alternative method and data set for calculating standard state properties relevant for the deep crust. Dolejš and Manning (2010) presented a model for mineral dissolution based on the thermodynamic and volumetric properties of the aqueous solvent; it is applicable up to 1100 °C and 2.0 GPa. The extended Debye–Hückel equation is commonly used to estimate the activities of charged species, although it cannot be applied to highly concentrated brines (Sverjensky, 1987). Activity coefficients for neutral species are assumed to be in unity or, in some cases, are modeled using the Satchenow equation (e.g., Sverjensky, 1987; Xie and Walther, 1993). The activity of H2O remains close to unity if the salt content is low (Sverjensky, 1987) but decreases markedly in concentrated brines (Aranovich and Newton, 1996, 1997). An important area of future research is the experimental and theoretical investigation of activity–composition relations for aqueous species in fluids that contain considerable CO2, CH4, and H2S.

Experimental, fluid inclusion, and field-based evidence indicates the following four generalized groupings of elemental abundances for fluids in typical quartz-bearing rocks at moderate pressures (~0.5 GPa): (1) Cl, Na, K, and Si; (2) Ca, Fe, and Mg; (3) Al; and (4) high-field-strength elements (HFSE), like zirconium, titanium, and rare earth elements (REE). Abundances are generally highest in the first group and lowest in the last. The concentrations of silicon, potassium, and sodium are relatively large in crustal fluids that coexist with quartz, feldspars, and/or micas. Aqueous silica concentrations in equilibrium with quartz increase markedly with T and P (Anderson and Burnham, 1965; Kennedy, 1950; Weill and Fyfe, 1964). Manning (1994) performed experiments at high P and T and combined the results with those of the previous studies to obtain an expression for silica molality applicable to ~900 °C and at least 2 GPa (Figure 6(b)). At deep-crustal conditions, quartz solubility decreases as the NaCl content of the fluid increases, and drops very sharply with the addition of CO2; thus, if immiscible brine–CO2 fluids exist in the deep crust, then silica will partition strongly into the brine (Figure 6(c): Newton and Manning, 2000a, 2000b; Walther and Orville, 1983). The effective solubility of albite also increases with P and T and decreases with increasing NaCl, although it should be noted that its dissolution is incongruent (Shmulovich et al., 2001). The behavior of aqueous silica, which is present mainly as the neutral H2SiO4~ complex, differs from that of sodium and potassium, which are present mostly as the charged species Na⁺ and K⁺ and the neutral chloride complexes NaCl⁻ and KCl⁻. Consequently, the total concentrations of sodium and potassium generally increase as the total concentration of chlorine increases in typical mica-bearing quartzofeldspathic rocks (Figure 6(d); e.g., Hauzenberger et al., 2001).

Calcium, magnesium, and iron are also present mostly as charged species or chlorine complexes and can reach relatively high concentrations in some fluids, particularly those coexisting with metatulmatitic and calcium silicate-bearing carbonatite rocks (e.g., Dipple and Ferry, 1992a; Ferry and Dipple, 1991; Vidale, 1967). A study of the incongruent dissolution of diopside shows that its effective solubility increases with increasing NaCl content, owing mostly to complexing of calcium and magnesium with chlorine in solution (Shmulovich et al., 2001). The retrograde solubility of calcite at low P and T is well known, but surprisingly, much remains to be learned about calcite behavior in the deep crust. The results of Dolejš and Manning (2010), however, indicate that calcite solubility in H2O is considerable – for example, ~1100 ppm at 600 °C and 1 GPa.

The concentration of aluminum is traditionally regarded as small in aqueous fluids (Figure 6(d)). However, complexing with alkalai and/or halides (Diakonov et al., 1996; Tagirov and Schott, 2001; Walther, 2001) and polymerization with aqueous silica and/or alkalai (Manning, 2006, 2007; Manning et al. 2010; Salvi et al., 1998; Wohlers and Manning, 2009) increases the concentration of aluminum in aqueous solutions, particularly at the high-P–T conditions relevant for the deep crust. For example, total aluminum concentrations at 700 °C and
concentrations (molality) calculated for the dominant species (aqueous $H_4SiO_4$ and $1.0 \text{ GPa.}$ Dashed lines depict mineral stabilities in terms of fluid $H_4SiO_4$ kyanite (Manning, 2007; Thompson, 2001). In addition, polymerization can increase other aluminum-rich phases in syn-metamorphic veins (e.g., Ague, 2001; Austrheim, 1990; Bucholz and Ague, 2010; possibilities (e.g., Ague, 2003; Ayers and Watson, 1991; Giere, 1990, 1993; Gieré and Williams, 1992; Jiang et al., 2005; Ohr et al., 1994; Pan and Fleet, 1996; Whitney and Olmsted, 1998).

REE can be transported by crustal fluids, but much remains to be learned about the processes and fluid chemistry involved (e.g., Grauch, 1989). The REE hosts monazite and apatite have relatively low solubilities in $H_2O$ (Antignano and Manning, 2008b; Ayers and Watson, 1991). Fluorapatite solubility increases with $P$, $T$, and fluid NaCl content (Antignano and Manning, 2008b).

Fluorine, phosphorus, yttrium, or other agents might complex HFSE, thus enhancing their transport in crustal fluids; radiation damage in zircon might increase its solubility, and titania and ilmenite might be more soluble than rutile, but much experimental and field work is needed to assess these possibilities (e.g., Ague, 2003; Ayers and Watson, 1991; Gieré, 1990, 1993; Gieré and Williams, 1992; Jiang et al., 2005; Ohr et al., 1994; Pan and Fleet, 1996; Whitney and Olmsted, 1998).

A number of laboratory- and field-based studies indicate that fluids and silicate melts can be completely miscible under appropriate conditions. For example, Bureau and Keppler (1999) observed experimentally complete miscibility between silicate melt and hydrous fluid for a variety of melt compositions and concluded that complete miscibility is possible in all but the shallowest parts of the upper mantle. Their results imply that amphibole breakdown in subduction zones should produce the mobile, hydrous fluids necessary for arc magma genesis, whereas breakdown of lawsonite or phengite deeper in subduction zones should produce much less mobile, silicate-rich fluids (see Chapters 4.19 and 4.20). While the results of Bureau and Keppler (1999) apply to relatively high-pressure settings, Thomas et al. (2000) showed that melt–fluid miscibility is possible even in low pressure (~0.1 GPa) pegmatite environments if the system is rich in fluorine, boron, and phosphorous. The recognition of significant miscibility opens up a host of new research avenues for melt–hydrous fluid systems, including their compositions, phase relations, physical and transport properties, and impact on the chemical evolution of the crust and mantle.

4.6.6 Chemical Transport and Reaction

4.6.6.1 Mass Fluxes

The processes of advection, diffusion, and mechanical dispersion transport chemical species in fluids. For a porous medium, the flux $F_i$ of species $i$ in the $x$, $y$, and $z$ coordinate directions (mol m$^{-2}$ (rock) s$^{-1}$) can be written:

$$F_i = v_i \phi C_i - D_{i, \text{f}} \phi \nabla C_i - D_{i, \text{a}} \phi \nabla C_i$$

[5]

in which $C_i$ is the concentration of $i$ in mol m$^{-3}$ (fluid). $D_{i, \text{f}}$ is the diffusion coefficient for $i$ through a free fluid, $\bar{\tau}$ is the tortuosity.
Nucleation rate

Characteristic length scale (m)

Symbols for chemical mass transfer and reaction rates

\( K_0 \) Equilibrium constant (dissolution reaction for phase \( \theta \))

\( L \) Characteristic length scale (m)

\( L_{AB} \) Distance of geochemical front propagation (m)

\( N_m \) Reaction order for reaction \( m \)

\( n_i \) Moles produced/consumed per unit volume rock (mol m\(^{-3}\))

\( \eta \) Nuclear rate

\( n, M, N \) Constants for rate expressions

\( P_s \) Peclet number

\( Q_i \) Ion activity product

\( R \) Gas constant (J mol\(^{-1}\) K\(^{-1}\))

\( R_{cm} \) Consumption/production rate of \( i \) (mol m\(^{-3}\) s\(^{-1}\))

\( r_{\theta} \) Dissolution/precipitation rate for \( \theta \) (mol m\(^{-3}\) s\(^{-1}\))

\( s \) Sign

\( T^* \) Kinetic reference temperature (K)

\( T_{eq} \) Equilibrium temperature (K)

\( V_i \) Molar volume of fluid (m\(^3\) mol\(^{-1}\))

\( V_{QZ} \) Molar volume of quartz (m\(^3\) mol\(^{-1}\))

\( \chi_i \) Mole fraction of \( i \) in fluid

\( \chi_{eq} \) Equilibrium mole fraction in fluid

\( a_L \) Longitudinal dispersivity (m)

\( a_T \) Transverse dispersivity (m)

\( \kappa \) Rate constant (s\(^{-1}\))

\( \kappa_m \) Intrinsic rate constant for reaction \( m \) (mol m\(^{-2}\) s\(^{-1}\))

\( \kappa_{\theta} \) Intrinsic dissolution/precipitation rate constant for phase \( \theta \) (mol m\(^{-2}\) s\(^{-1}\))

\( v_{m,\theta} \) Stoichiometric coefficient for \( i \) in reaction \( m \)

\( \xi \) Tortuosity tensor

\( \tau \) Tortuosity (constant)

### Table 2

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition and SI units</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i )</td>
<td>Subscript denoting fluid species ( i )</td>
</tr>
<tr>
<td>( m )</td>
<td>Subscript denoting reaction ( m )</td>
</tr>
<tr>
<td>( \theta )</td>
<td>Subscript denoting solid phase ( \theta )</td>
</tr>
<tr>
<td>( A_{m,i} )</td>
<td>Surface area of rate-limiting mineral ( i ) in reaction ( m ) (m(^2) m(^{-3}))</td>
</tr>
<tr>
<td>( A_\theta )</td>
<td>Reactive surface area of ( \theta ) (m(^2) m(^{-3}))</td>
</tr>
<tr>
<td>( \delta_i )</td>
<td>Activity of species ( i )</td>
</tr>
<tr>
<td>( \chi_i )</td>
<td>Concentration of ( i ) in fluid (mol m(^{-3}))</td>
</tr>
<tr>
<td>( \chi_{eq} )</td>
<td>Concentration of ( i ) in solid (mol m(^{-3}))</td>
</tr>
<tr>
<td>( D_{HID,ij} )</td>
<td>Hydrodynamic dispersion tensor (m(^2) s(^{-1}))</td>
</tr>
<tr>
<td>( D_{DID,ij} )</td>
<td>Hydrodynamic dispersion coefficient (m(^2) s(^{-1}))</td>
</tr>
<tr>
<td>( D_i )</td>
<td>Diffusion coefficient for ( i ) in fluid (m(^2) s(^{-1}))</td>
</tr>
<tr>
<td>( D_M )</td>
<td>Mechanical dispersion tensor (m(^2) m(^{-3}))</td>
</tr>
<tr>
<td>( E_a )</td>
<td>Activation energy (J mol(^{-1})</td>
</tr>
<tr>
<td>( F_i )</td>
<td>Flux vector for species ( i ) (mol m(^{-2}) s(^{-1}))</td>
</tr>
<tr>
<td>( \Delta G )</td>
<td>Gibbs free energy change for reaction (J mol(^{-1}))</td>
</tr>
<tr>
<td>( K_s )</td>
<td>Equilibrium fluid/solid partition coefficient by volume (mol m(^{-3}) fluid)/(mol m(^{-3}) solid)</td>
</tr>
<tr>
<td>( K_{\theta} )</td>
<td>Equilibrium constant (dissolution reaction for phase ( \theta ))</td>
</tr>
<tr>
<td>( L )</td>
<td>Characteristic length scale (m)</td>
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<tr>
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<td>Intrinsic rate constant for reaction ( m ) (mol m(^{-2}) s(^{-1}))</td>
</tr>
<tr>
<td>( \kappa_{\theta} )</td>
<td>Intrinsic dissolution/precipitation rate constant for phase ( \theta ) (mol m(^{-2}) s(^{-1}))</td>
</tr>
<tr>
<td>( v_{m,\theta} )</td>
<td>Stoichiometric coefficient for ( i ) in reaction ( m )</td>
</tr>
<tr>
<td>( \xi )</td>
<td>Tortuosity tensor</td>
</tr>
<tr>
<td>( \tau )</td>
<td>Tortuosity (constant)</td>
</tr>
</tbody>
</table>

The pathways for diffusion between grains through an interconnected porosity are not straight, but are instead complex and tortuous. Consequently, diffusion through rock is slower than that through a free fluid; the tortuosity tensor is introduced to describe this behavior. Tortuosity is expressed as a tensor because it can vary with direction. Tortuosity systematics for metamorphic rocks are largely unknown, but it seems likely that pathways will be less tortuous parallel to penetrative fabrics than perpendicular to them. Ague (1997a) found that diffusion adjacent to a cross-cutting quartz vein occurred more readily in metapelitic layers than metapsammitic ones; the difference may reflect less tortuosity parallel to micaceous fabrics in the metapelites relative to the metapsammites. In theory, tortuosity can vary between 1 (perfectly straight pathways) and near 0. Values measured in porous media range from about 0.3 to 0.6 (Bear, 1972, p. 111), consistent with measurements of diffusion through pores in granodiorite (Fisher and Elliott, 1973), but much remains to be learned regarding tortuosity during active metamorphism.

Length scales of coupled diffusion and reaction can be considerable. Diffusion of mass across contacts between meta-pelitic and metacarbonate rocks can drive reactions that produce calc-silicate reaction zones on the centimeter to meter scale (e.g., Ague, 2002; Brady, 1977; Thompson, 1975; Vidale, 1969; Vidale and Hewitt, 1973). Bickle et al. (1997) estimated an ~5–10 m length scale for the diffusional component of oxygen isotope exchange across a lithologic contact. Characteristic length scales for reactive strontium diffusion across the lithologic contacts studied by Bickle et al. (1997) and Baxter and DePaolo (2000) are ~2 and ~0.7 m, respectively. Numerical models suggest ~1–10 m length scales may be relevant for the exchange of H\(_2\)O and CO\(_2\) between adjacent layers, particularly if the product \( \phi r > 5 \times 10^{-5} \) (Ague, 2000, 2002; Ague and Rye, 1999). Field tests confirm volatile mass exchange over such length scales in the deep crust (Ague, 2003; Ferry, 2008; Pennistort-Dorland and Ferry, 2006). Extremely fluid-mobile elements, such as lithium, can have diffusional transport distances as large as ~30 m (Liu et al., 2010; Teng et al., 2006).

Diffusion transports mass down concentration gradients (from regions of high concentration to low concentration) according to eqn [5], although it is actually driven by gradients in chemical potential (e.g., Shewmon, 1969). The concentration gradient-based approach turns out to be accurate for most tracers. It is generally used for species at higher concentrations as well, but complications, including the dependence of diffusion coefficients on fluid composition and diffusion up concentration gradients, can arise as the diffusing species interact subject to their chemical potential gradients and mass and charge balance constraints. The papers of Graf et al. (1983) and Liang et al. (1996) illustrate some of the problems that need to be solved in future studies of complex diffusional behavior during metamorphism.

Mechanical dispersion of transported species occurs during fluid flow, increases as flow velocity increases, and arises because (1) fluid in adjacent porous pathways will be moving at slightly different velocities and (2) the tortuous nature of the flow paths causes mixing. Because of its dissipative nature, mechanical dispersion is generally modeled using a mathematical form identical to that for diffusion, although the processes underlying diffusion and mechanical dispersion are very limited by porosity and tortuosity (eqn [5]).
can be used, where $a_{x}$ and $a_{y}$ are the coefficients of longitudinal and transverse dispersivity, respectively (Bear, 1972). The $a_{i}|v_{i}$ term describes mechanical dispersion parallel to $x$, whereas the $a_{i}|v_{i}$ terms describe it parallel to $y$ and $z$. Longitudinal dispersivity can vary over several orders of magnitude in natural geologic materials (Garven and Freeze, 1984b). It is another variable that is not well known for metamorphism, but by analogy with low-permeability rocks, like shales, values between near 0 and $\sim 10$ m appear reasonable (Ague, 2000). The transverse dispersivity is expected to be as much as two orders of magnitude smaller (Garven and Freeze, 1984b). When diffusion and mechanical dispersion act together, length scales of mass transfer can be considerable; Ferry (2008) documents cross layer transport of $H_{2}O$-$CO_{2}$ over distances $>70$ m. Note that if the medium is anisotropic, then significant complexities are introduced into the tensor representation of mechanical dispersion (Bear, 1972).

### 4.6.6.2 Reaction Rates

The fluid infiltration histories of fossil metamorphic flow systems are recorded when the fluid reacts with the rock. If there was no reaction during flow, then fluxes could be large but the rock would not preserve evidence of the flow. Furthermore, the presence or absence of water is a critical factor in determining element mobility and, hence, rates of crustal reaction (e.g., Carlson, 2010). In a classic example, Austrheim (1987, 1990) documents dry, Precambrian granulite facies rocks that were metastable in the lower crust until infiltrated by hydrous fluids during Caledonian orogenesis. The infiltration occurred along shear zones, veins, and other permeable zones, converting anhydrous granulite facies assemblages to eclogite facies ones formed when fluid that flowed along the vein infiltrated into the host anorthosite under eclogite facies conditions. The anorthosite that was not infiltrated remained metastable under high-pressure conditions and did not react to form eclogite facies mineral assemblages. Reproduced from Austrheim H (1990) The granulite–eclogite facies transition: A comparison of experimental work and a natural occurrence in the Bergen Arcs, western Norway. Lithos 25: 163–169. With permission from Elsevier.

Precipitating or dissolving areas of the mineral is slow relative to transport rates through the solution surrounding the grain, the rate is said to be surface controlled. The opposite case of fast attachment or removal relative to transport is called transport controlled or sometimes diffusion controlled. Consider a quartz crystal bathed in fluid. For surface-controlled rates, the concentration of aqueous silica species at the surface of the mineral is identical to that in the surrounding bulk solution. Note that these concentrations need not be at equilibrium values. On the other hand, for transport control by diffusion, the concentrations of aqueous silica species at the surface of the quartz are at equilibrium values, but concentration gradients exist between the solution composition at the surface and the composition in the surroundings. Either surface or transport control can be dominant, depending upon the nature of the reaction–transport system (e.g., Sanchez-Navas, 1999); a number of studies suggest dominance of surface control in many common fluid–rock settings (e.g., Steefel and Lasaga, 1994), but a more complex behavior is also possible (Dohmen and Chakraborty, 2003).

A wide array of experimental studies indicate that rates of mineral dissolution and precipitation in aqueous solution are controlled primarily by reactive surface area, rate constants, activities of catalyzing/inhibiting agents, and departures of Gibbs energy from equilibrium. The relationships between these factors can be described by the following generalized rate law, which is consistent with the transition state theory (see Steefel and Lasaga, 1994; and references therein):

\[
\text{Rate} = A_{\theta}k_{\theta}f(A\Gamma) \tag{7}
\]

in which $A_{\theta}$ is the reactive surface area of mineral $\theta$ in units of area mineral per unit volume rock, $k_{\theta}$ is an intrinsic rate constant in units of moles mineral per unit area per time; $f(a_{i})$ is a function of the activities of aqueous species $i$ in
solution, which act to either catalyze or inhibit reaction; and $f(\Delta G)$ is some function of the free energy of the system. A more specific form of eqn [7] that is generally applicable to surface-controlled reactions among common minerals is

$$r_\theta = sA_i\kappa_\theta \left( \prod_i a_i^{\delta_i} \right) \frac{Q_0}{K_\theta} M^N$$

in which $r_\theta$ is the dissolution or precipitation rate for $\theta$ in moles per unit volume rock per unit time; $p$ is an experimentally determined constant; $M$ and $N$ are two positive numbers also generally determined by experiment; $Q_0$ is the ion activity product; $K_\theta$ is the equilibrium constant for the reaction ($Q_0$ and $K_\theta$ are equal at equilibrium); and $s$ is, by convention, negative if the solution is undersaturated with respect to $\theta$ and positive if supersaturated (Steefel and Lasaga, 1994). If $M$ and $N$ are both one, then the rate law is said to be linear; otherwise, it is nonlinear. The intrinsic dissolution or precipitation rate constant $\kappa_\theta$ is strongly $T$-dependent and is usually expressed as an Arrhenius-type equation (e.g., Oxtoby et al., 1999):

$$\kappa_\theta = \kappa_0^\theta \exp \left( \frac{-E_a}{R} \left( \frac{1}{T} - \frac{1}{T^0} \right) \right)$$

in which $E_a$ is the activation energy and $T^0$ is the reference temperature (often 298.15 K). With this kinetic behavior, reaction rates will increase by a factor of 30–90 kJ mol$^{-1}$ for common silicate and carbonate minerals, averaging around 60 kJ mol$^{-1}$. The dissolution or precipitation reaction that the rate expression [9] is keyed into is usually written for 1 mol of mineral, for example, for K-feldspar, one could write $\text{KAlSi}_3\text{O}_8 + 4\text{H}^+ = K^+ + \text{Al}^{3+} + 3\text{SiO}_2\text{aq} + 2\text{H}_2\text{O}$. Dissolution proceeds from right to left and precipitation from left to right; at equilibrium, both rates are equal. The rates of reaction among the species in solution are commonly assumed to be instantaneous (e.g., Helgeson, 1979; Sverjensky, 1987).

The overall rate of a fluid–rock reaction can also be modeled rather than computing the dissolution and precipitation of each solid separately. For example, one could write an overall reaction between solids and fluids, such as muscovite + quartz = sillimanite + K-feldspar + H$_2$O (Schramke et al., 1987). The model for overall reactions in metamorphic rocks advanced by Lasaga and Rye (1993) includes all the basic pieces of eqn [7] except the catalysis/inhibitor term (Ague, 1998):

$$R_{i,m} = \left( \frac{1}{\Theta} \right) sK_{im}v_m \tilde{A}_{im} |\Delta G_{im}|^{N_m}$$

in which $R_{i,m}$ is the rate in moles of $i$ per unit volume fluid per unit time for reaction $m$; $\kappa_{im}$ is the intrinsic reaction rate constant; $v_{im}$ is the stoichiometric coefficient for $i$; $\tilde{A}_{im}$ is the surface area of the rate-limiting mineral $l$ per volume rock in reaction $m$; $|\Delta G_{im}|$ is the absolute value of the Gibbs free energy change of reaction $m$ at the $T$ and $P$ of interest; $N_m$ is the reaction order; and $s$ is, by convention, +1 if $\Delta G_{im}$ is negative and −1 otherwise. If $N_m = 1$, then the rate law is linear; otherwise, it is nonlinear. Lütte et al. (2004), for example, apply kinetic theory and discuss intrinsic rate constants relevant for metamorphism of silicic dolomites. Note that eqn [10] gives the production/consumption rate for moles of a fluid species $i$, whereas eqn [8] is written for moles of solid. The net production/consumption rate for $i$ is obtained by summing over the rate expressions for all reactions $m$.

In general, the rate-limiting surface area, $\tilde{A}_{im}$, in the overall rate eqn [10] is determined by the mineral with the slowest surface reaction kinetics and the lowest surface area in contact with fluid. $\tilde{A}_{im}$ is thus a function of critical rock physical properties, including the rock porosity structure and the size, shape, and abundance of mineral grains. Much progress has been made by estimating mineral surface areas using simple geometric shapes, like spheres or cubes, that grow or shrink during reaction (Bolton et al., 1999; Steefel and van Cappellen, 1990). However, the amount of reactive surface area remains as one of the major uncertainties in modeling reaction rates.

A simpler but useful expression has been widely used in geochemistry to model reaction rates:

$$R_i = \kappa(C_i^{eq} - C_i)^N$$

The reaction rate is proportional to the difference in concentration between the fluid in contact with the mineral assemblage at a particular place in the system ($C_i$) and the fluid composition that would be in equilibrium with the mineral assemblage ($C_i^{eq}$). Thus, the net rate is 0 when fluid and rock are at chemical equilibrium ($C_i = C_i^{eq}$). The rate constant $\kappa$ actually combines several key rate variables and, for linear
rates ($N=1$), can be cast in terms of the product of the intrinsic reaction rate constant, a reactive surface area term, and the derivative of the $\Delta G$ of reaction with respect to concentration (Lasaga and Rye, 1993).

In real rocks, dissolution, precipitation, and devolatilization reactions proceed only if there is some departure from local fluid–rock equilibrium, a condition known as overstepping. Models of fluid–rock reaction that use the local equilibrium approximation assume that reaction rates are so fast as to be essentially instantaneous. However, for some reactions, such as those with small intrinsic rate constants and small reactive surface areas, the rate of reaction near equilibrium is slow. Consequently, the $T$, $P$, and/or fluid composition must depart significantly from equilibrium before $\Delta G$ (the driving force for reaction) is large enough to produce significant rates. The magnitude of the overstepping is likely to be larger if the reaction rate law is nonlinear (eqns [8]–[11]).

Overall rate expressions, like eqn [10], assume reactants and products are present and reacting, with the degree of overstepping being controlled by the rate at which the transformation of reactants into products occurs. Equilibrium is also overstepped if product solids fail to nucleate (e.g., Jamtveit and Anderson, 1992; Pattison and Tinkham, 2009; Putnis and Holland, 1986; Rubie, 1998; Waters and Lovegrove, 2002; Wilbur and Ague, 2006). Classical theory holds that when a new phase nucleates, extra energy is necessary to form the grain boundary between the new phase and the phases from which it is growing (e.g., Shewmon, 1969). At equilibrium, this extra energy is unavailable and no growth of reaction products occurs. Overstepping of the equilibrium condition, however, provides the energy necessary to nucleate and grow reaction products and decrease the overall free energy of the system. For the cases of $T$ and fluid composition (X) overstepping, the nucleation rate $n$ is proportional to (Ridley and Thompson, 1986):

$$n \propto \exp (T - T_{eq})^2$$  \[12\]

and

$$n \propto \exp (X - X_{eq})^2$$  \[13\]

in which $T_{eq}$ and $X_{eq}$ are equilibrium temperature and fluid composition, respectively. Thus, once the products do nucleate in an overstepped reaction, it is likely that they will do so readily, given the exponential and power terms in these expressions. It appears that some phases, particularly garnet solid solutions, continue to nucleate well after the exponential stage, albeit at considerably reduced rates (e.g., Carlson, 1989).

The rates of metamorphic reactions and the magnitude of departures from local chemical equilibrium are important and controversial issues in the Earth sciences today. Fluid fluxes, $P$-$T$ time evolution, and reaction histories estimated assuming local equilibrium models would clearly be in error if the actual processes operated far from equilibrium. Some examples of chemical disequilibrium, such as sluggish phase transformations among the Al$_2$SiO$_5$ polymorphs and selective retrograde reaction along pathways of fluid infiltration, have been well documented (e.g., Giogetti et al., 2000; Kerrick, 1990). Other concrete examples of chemical disequilibrium for prograde metamorphic devolatilization reactions and fluid flow are still relatively rare, but the number is steadily increasing as theoretical, textual, isotopic, and field studies focus on the problem (e.g., Baxter and DePaolo, 2000, 2002ab; Chernoff and Carlson, 1997; Jamtveit, 1992; Lütte et al., 2004; Müller et al., 2004; Pattison and Tinkham, 2009; Pattison et al., 2011; Putnis and Holland, 1986; Waters and Lovegrove, 2002; Wilbur and Ague, 2006). It is common to observe variable grain sizes for a given mineral in a metamorphic rock. Such textures are inconsistent with equilibrium (Thompson, 1987), but it is unclear if they indicate large energetic departures from equilibrium. Laboratory evidence strongly suggests that the degree of prograde $T$ overstepping due to nucleation problems may be on the order of 10–100 K and 1–10 kJ, with the smallest values for devolatilization reactions and the largest for reactions with small entropy changes such as solid–solid reactions (Ridley and Thompson, 1986). $P$ oversteps may be 0.1 GPa or more (Ernst and Banno, 1991; Ridley and Thompson, 1986). When multiple product phases must nucleate, oversteps are likely to be large and may exceed ~0.7 GPa (Rubie, 1998). If devolatilization reactions are overstepped significantly in $T$, then the subsequent rapid reaction that occurs upon nucleation and mineral growth may generate large fluid pressures sufficient to drive hydrofracture and fluid flow (e.g., Ague et al., 1998; Walther, 1996) over short timescales of 10–10$^3$ years (Ague et al., 1998).

Theoretical calculations suggest that slow rates may cause significant reaction overstepping in metacarbonate rocks, consistent with observed oxygen and carbon isotopic disequilibrium in some contact aureoles (Lütte et al., 2004; Müller et al., 2004). A particularly insidious problem here is that sequences of mineral assemblages produced in the field relatively far from equilibrium can mimic local equilibrium sequences (Lütte et al., 2004).

Baxter and DePaolo (2000, 2002a,b) measured mineral chemistry and strontium isotope systematics for garnet and whole rock across a lithologic contact near Simplon Pass, Switzerland, and concluded that rates of reaction during cooling from ~610 to ~500 °C were extremely small, amounting to roughly 10$^{-7}$ g solid reacted per gram of rock per year. The slow reaction rates may reflect, in part, the cooling regime of retrograde metamorphism when fluids are not abundant, but Baxter and DePaolo (2000) also argue that prograde rates could not have been fast either. One provocative implication is that the chemical systematics of minerals that participate in such slow reactions may be unable to track changes in fluid chemistry, $P$, and $T$ (Baxter and DePaolo, 2002b). In summary, mounting field, laboratory, and theoretical evidence indicates that chemical kinetics may be an important control on metamorphic processes, so it is prudent to examine the assumption of equilibrium before using it.

### 4.6.6.3 Transport and Reaction Within Crystals

Thus far, mass transport and reaction around grains through fluid-filled pore spaces and cracks, but not within the grains themselves are considered. At low to moderate metamorphic grades, intracrystalline (within grain) diffusion is commonly assumed to be slow enough, relative to fluid-mediated transport and reaction, that it can be neglected. Nonetheless, in cases of slow fluid transport, diffusive transfer into and out of
grains could have a more significant impact on fluid geochemistry, particularly at high-temperature conditions where diffusion rates are enhanced. Although intracrystalline diffusion effects may be limited, a growing body of evidence indicates that mass transport to and from crystals by coupled dissolution and precipitation (referred to here as CDP) can operate rapidly enough to influence the chemical and isotopic compositions of crystals and migrating fluids over a wide range of crustal conditions (Dumond et al., 2008; Harlov et al., 2005; Labotka et al., 2004; O’Neill and Taylor, 1967; Putnis, 2002; Putnis and John, 2010).

CDP requires that a disequilibrium fluid comes into contact with crystal surfaces (Figure 10). Chemical reaction involving recrystallization then replaces the existing mineral with a new one in equilibrium with the fluid. This reaction interface then propagates into the crystal. As it does, it leaves behind a zone of fluid-filled, micro- or nanoscale porosity in the replaced mineral; these zones have been clearly documented in experimental studies and some field studies (Putnis and Austreheim, 2010; Putnis and John, 2010). Reactants are transported into, and products out of, such porous zones, facilitating the inward movement of the replacement front. The transport could be by diffusion, advection, or some combination. Porosity may be generated if the overall replacement reaction has a negative volume change and/or if the rate of dissolution is faster than the rate of precipitation. A key point is that because transport is dominantly through a fluid-filled porous network in the replaced crystal, rates of mineral change are orders of magnitude faster than they would be if controlled by solid-state intracrystalline diffusion alone. Another key point is that the replacement fronts are extremely sharp, much sharper than normally expected for intracrystalline diffusion (Figure 11).

When parent and product minerals share some common crystallographic relationships, nucleation of the product is likely to be epitaxial (Putnis, 2002). This can result in pseudomorphic replacement. Experimental examples of albite replaced by K-feldspar, and replacement reactions involving apatite are shown in Figure 11(a) and 11(b). In cases where there is less lattice matching, reaction products will normally be polycrystalline and lack epitaxial relationships (Figure 11(c)).

CDP processes have major implications for interpretation of fluid–rock reactions in the geologic record (see Putnis and John, 2010). One is that the parent and product phases are probably not in chemical equilibrium with each other. Consequently, it is hazardous to use equilibria involving parent–product compositions to estimate pressures, temperatures, or fluid compositions. The most likely equilibrium is between the interfacial fluid and the product phase (Putnis and John, 2010). Another

---

**Figure 10** Schematic illustration of coupled dissolution–precipitation (CDP). (a) Original parent crystal. (b) Original crystal partially replaced on rims and along crack. Reaction interfaces propagate inward as reactants are transported in, and products out, through a network of fluid-filled micro- or nanopores in the replaced crystal.

implication is that CDP processes operate quickly, even on laboratory timescales – essentially instantaneous geologically. This speed means that CDP reactions could track both the timing and compositional evolution of infiltrating fluids much more rapidly than intracrystalline diffusion and, thus, preserve a more detailed record of the fluid–rock interaction. Indeed, recrystallization of monazite has been shown to record a wide array of tectonometamorphic episodes in rocks with geologically complex histories (Catlos et al., 2002; Dumond et al., 2008; Martin et al., 2007). A further implication is that modeling of closure temperatures will be complicated in crystals that contain isotopic variations resulting from CDP instead of, or in addition to, intracrystalline diffusion (Villa, 2006).

If CDP processes do not go to completion, leaving some unreacted original crystal behind (Figure 11), then intracrystalline diffusion will tend to smooth the sharp chemical and isotopic boundaries between parent and product material through time. The rate at which this happens depends strongly on temperature and the intracrystalline diffusion characteristics of the minerals involved (see Chapter 4.7). Modeling of the timescales necessary to produce partially relaxed diffusion profiles stranded between crystal cores and rims can then place constraints on thermal histories following the cessation of CDP (e.g., Watson and Baxter, 2007).

4.6.6.4 Advection–Dispersion–Reaction Equation

A fundamental task of fluid–rock studies is to determine the infiltration and reaction histories of rocks at any given point in a flow system. Imagine that the flow region of interest comprises infinitesimally small, cube-shaped building blocks or control volumes that are interconnected. The goal is then to quantify the changes in the masses of fluid species within each control volume due to net advection and hydrodynamic dispersion of fluid into or out of the volume and the consumption or production of species within the volume due to internal chemical reactions. The required partial differential equation describing mass conservation for a fully saturated porous medium has been derived by many workers (e.g., Bear, 1972; DeGroot and Mazur, 1969; Fletcher and Hofmann, 1973; Garven and Freeze, 1984a; Guenther and Lee, 1988). It is based on the flux eqn [5] and includes a term for chemical reaction:

\[
\frac{\partial (C_i \phi)}{\partial t} = \nabla \cdot (D_i \nabla C_i) + \nabla \cdot (\nu D_i \phi \nabla C_i) + \phi \sum_m R_{m,i} \quad [14]
\]

in which \(R_{m,i}\) is the production rate (positive) or consumption rate (negative) for species \(i\) in reaction \(m\) (e.g., eqn [10]), and diffusion and mechanical dispersion have been combined into a single hydrodynamic dispersion tensor \((D_i) = D_i (\phi \nabla \cdot \nabla) + D_{\text{AB}}\).

Terms (a), (b), and (c) describe advection, hydrodynamic dispersion, and reaction, respectively, and the left hand side gives the total change in the moles of species \(i\) in the fluid per unit volume rock per unit time. Partial differential eqn [14] is known as the advection–dispersion–reaction equation, and as written, it has an infinite number of solutions. It can be solved for individual cases by specifying initial conditions and boundary conditions that describe the flow system. The rock medium through which the fluid flows is assumed to be stationary; additional terms are required if the rock moves as well.

4.6.7 Geochemical Fronts

One common reaction–transport scenario arises when fluid that is out of equilibrium with a rock mass of interest infiltrates across a boundary and drives reaction. The boundary could be, for example, a lithologic contact between two chemically and/or isotopically distinct kinds of rock or the contact between the rock and a fracture through which fluid flows. Equation [14] is valid for general transport–reaction problems, but even a one-dimensional version with constant pore velocity, hydrodynamic dispersion, porosity, and rate constant exhibits significant complexity and illustrates fundamental principles:

\[
\frac{\partial C_i}{\partial t} = -\nu \frac{\partial C_i}{\partial x} + D_{\text{HD},i} \frac{\partial^2 C_i}{\partial x^2} + \kappa (C_i^{\text{eq}} - C_i) \quad [15]
\]

The concentration of \(i\) in the solid, \(C_i^{\text{solid}}\), is given by

\[
\frac{\partial C_i^{\text{solid}}}{\partial t} = -\kappa \frac{\phi}{1 - \phi} (C_i^{\text{eq}} - C_i) \quad [16]
\]

For nonreactive transport with \(\kappa = 0\), a constant input concentration of \(C_{i,x=0}\) at the \(x=0\) boundary (boundary condition), and an initial concentration of \(C_i = 0\) throughout the flow domain (initial condition), the analytical solution to eqn [15] is well known (Fried and Combarnous, 1971):

\[
\frac{C_i}{C_{i,x=0}} = \frac{1}{2} \left( \text{erfc} \left( \frac{x - \nu t}{2 \sqrt{D_{\text{HD},i} t}} \right) + \exp \left[ \frac{\nu x}{D_{\text{HD},i}} \right] \text{erfc} \left( \frac{x + \nu t}{2 \sqrt{D_{\text{HD},i} t}} \right) \right) \quad [17]
\]

in which \text{erfc} is the complimentary error function. Equation [17] gives the concentration of \(i\) at any point and time in the flow region if there is no reaction and is a useful approximation for the transport of \(i\) from one layer to another across a model lithologic contact at \(x=0\). Several important concepts can be illustrated by first assuming that transport occurs only by flow and that hydrodynamic dispersion is negligible. As flow proceeds, the input fluid displaces more and more of the initial fluid in the direction of flow; the boundary between the input and displaced fluids is known as the infiltration front or hydrodynamic front and is marked by a sharp change in concentration referred to as a concentration front or solute front (Figure 12(a)). For constant \(\nu\), the distance of front travel over a time interval \(\Delta t\) is \(\nu \Delta t\). The time-integrated fluid flux \((q_{\text{RT}})\) is the total amount of fluid flow that passes across an area of interest during a given time interval; for this problem, it is simply \(\nu \phi \Delta t \left( m^3 \text{ fluid} \cdot m^{-2} \text{ rock} \right)\). Pioneering studies, including Baumgartner and Ferry (1991), Ferry and Dipple (1991), and Bickle (1992), demonstrated that the time-integrated fluid flux is invaluable for quantifying fluid–rock interactions (much more will be said about \(q_{\text{RT}}\) in the succeeding text). Hydrodynamic dispersion acts to smooth sharp concentration fronts, and the degree of front broadening increases the farther the front travels (Figure 12(b)). Finally, the characteristic concentration profiles for pure diffusion are shown in Figure 12(c).

The relative importance of advection relative to hydrodynamic dispersion is often assessed using the dimensionless Peclet number: \(P_e = \nu L / D_{\text{HD},i}\), in which \(L\) is the length scale of interest. Hydrodynamic dispersion tends to dominate for small
and kyanite in equilibrium with an aqueous pore fluid reacts. Consider a schematic example. A rock comprising corundum and kyanite in equilibrium with an aqueous pore fluid reacts with a fluid input at \( x = 0 \) that is in equilibrium with quartz and kyanite. At moderate metamorphic temperatures and pressures, dissolved aqueous silica will be the dominant species in solution. The input fluid has a larger activity of aqueous silica, so as it enters the flow region, silica is consumed as corundum breaks down by reactions such as SiO\(_2\)\,(aq) + corundum = kyanite. Reaction is removing \( i \) (aqueous silica) from the fluid, so the concentration of SiO\(_2\) in the bulk solid continually increases (e.g., Figure 13(b)). The fluid composition, however, is not steady state because the amount of \( i \) consumed at any given point is replenished by the amount transported to that point by advection and hydrodynamic dispersion (Figure 13(a)). These relations illustrate that one or more processes in a system may be in steady state, but others need not be. The boundary between the reacted and unreacted regions in the rock is known as a reaction front or a geochemical front. Eventually, all the corundum at the point of fluid input would be converted to kyanite, and the reaction and solute fronts would then begin to propagate out in the direction of flow (e.g., Figure 14). As a consequence, fossil geochemical fronts can provide valuable clues regarding the direction of fluid flow (e.g., Abart and Pozzorini, 2000; Baker and Spiegelman, 1995; Bickle, 1992; Bickle and Baker, 1990; Rye et al., 1976; Skelton et al., 1995). Note that when both fronts are moving, neither fluid nor rock compositions are steady state. For advection-dominated systems with small porosity (\(<0.01\)), the time-integrated fluid flux is approximated by (Agu, 1998)

\[
q_{\text{ff}} \approx \frac{L_{\text{CF}}}{C_{i}^{\text{eq}} - C_{i, x=0}^{\text{input}}} \cdot \frac{n_{i}}{C_{i}^{\text{input}}}
\]

where \( L_{\text{CF}} \) is the distance of geochemical front propagation in the rock. For example, \( C_{i, x=0}^{\text{input}} \) is the concentration of \( i \) (silica)
in the input fluid, whereas $n_i$ is the number of moles of $i$ produced ($+$) or consumed ($-$) per unit volume rock (mol m$^{-3}$). Of course, this highly reduced example neglects many factors, including the speciation of the multicomponent fluid and reaction mechanisms. In many cases, these complexities are not tractable with analytical solutions and require numerical modeling (e.g., Ague, 1998, 2000; Ague and Rye, 1999; Bolton et al., 1999; Cook et al., 1997; Nabelek, 2009).

The shapes of the fronts depend strongly on the reaction rate (Figure 15). If rates are fast, then $i$ is consumed rapidly and the solute front dies away close to the boundary where reactive fluid is input. By contrast, fronts broaden considerably as the rate decreases. Front broadening can occur even if hydrodynamic dispersion is absent and can be significant at $>100$ m length scales (Bickle, 1992). Dimensionless Damköhler numbers are often used to assess the relative roles of transport and reaction. For the case of advective transport, the Damköhler number is $kL/t_v$, and for transport by diffusion, it is $kL^2/\mathcal{D}_{ij}$ (Boucher and Alves, 1959). In either case, solute and geochemical fronts sharpen as the Damköhler number increases. If the rate of reaction is very fast (nearly instantaneous) relative to the rate of transport, then fluid and rock are essentially in chemical equilibrium at any given point along the flow path (the local equilibrium condition).

A somewhat different form of the reaction rate term in eqns [11] and [15] has been widely used for modeling transport of tracers, particularly isotopic tracers (e.g., Bickle, 1992; Bickle et al., 1997; Blattner and Lassey, 1989; DePaolo and Getty, 1996; Lassey and Blattner, 1988; Oagata, 1964):

$$\text{Rate} = \kappa \frac{1 - \phi}{\phi} \left( \frac{C_i^{\text{solid}} - C_i^{\text{f}}}{K_v} \right)$$

in which $K_v$ is the equilibrium fluid/solid partition coefficient by volume for species $i$ and $k$ has been interpreted as the rate constant for fluid–rock exchange (Bickle, 1992) or for dissolution and precipitation of mineral material (DePaolo and Getty, 1996). Here, as the bulk composition of the solid changes, so too does the composition of the fluid in equilibrium with the solid. For advective transport, tracer exchange according to eqn [19], and constant porosity and fluid velocity, the time-integrated fluid flux ($q_{\text{fit}}$) is approximated by $L_{\text{cr}}/K_v$ (Bickle, 1992). The $q_{\text{fit}}$ expression for transport by advection with coupled local fluid–rock equilibrium exchange $\pm$ hydrodynamic dispersion has exactly the same form (e.g., Bickle, 1992; Dipple and Ferry, 1992b). For example, if an oxygen isotopic front has propagated 1000 m and the $K_v$ for oxygen is 0.6, then the $q_{\text{fit}}$ estimate is $\sim1700$ m$^3$ (fluid) m$^{-2}$ (rock). Fronts for tracers with smaller $K_v$ would propagate smaller distances for the same flux, and vice versa. Interpretations become more complicated if $K_v$ changes with $T$ or the individual mineral grains become isotopically zoned during reaction (e.g., Abart and Sperb, 1997; Bowman et al., 1994; Ferry et al., 2010; Graham et al., 1998; Lewis et al., 1998). Radioactive decay is not considered in eqn [19] and must be handled with an additional term (DePaolo and Getty, 1996).

### 4.6.8 Flow and Reaction Along Gradients in Temperature and Pressure

In the examples thus far, fluid that is out of equilibrium with a rock mass of interest infiltrates across some type of lithologic boundary, drives reaction, and forms geochemical fronts. Reaction will also occur if fluid flows along gradients in $T$ and $P$ because fluid compositions coexisting with minerals change as $T$ and $P$ change. A classic example is the precipitation of quartz in fractures to form veins (Ferry and Dipple, 1991; Fyfe et al., 1978; Walther and Orville, 1982; Yardley, 1986). Precipitation occurs because the concentration of aqueous silica coexisting with quartz must decrease as $T$ and $P$ decrease along a flow path (Figure 6b). Imagine silica-saturated fluid ascending and cooling though a cubic control volume 1 m on a side. Fluid enters the bottom face of the cube and exits through the top. The concentration of aqueous silica at the inlet is higher than that at the outlet, since quartz is precipitating from the fluid within the control volume. Assume that this drop in concentration is $5 \times 10^{-3}$ mol m$^{-3}$ for a typical geothermal gradient (more will be said about this in the
The corresponding concentration gradient \((5 \times 10^{-3} \text{ mol m}^{-3} \text{ m}^{-1})\) is small, so fluxes due to hydrodynamic dispersion can be neglected. The amount of quartz needed to fill the control volume is equivalent to the molar volume of quartz \((-4.4 \times 10^{3} \text{ mol m}^{-3}\)). The time-integrated fluid flux can then be estimated by reinterpreting eqn [18] slightly:

\[
q_{T} \approx (1 \text{ m}) \frac{4 \times 10^{4} \text{ mol m}^{-3}}{5 \times 10^{-2} \text{ mol m}^{-1}} \approx 9 \times 10^{5} \text{ m}^{3} \text{ m}^{-2}
\]

\[20\]

Ferry and Dipple (1991) derived a more formal one-dimensional, local equilibrium, steady-state expression based on eqn [14] that neglects hydrodynamic dispersion and explicitly accounts for changes in concentration along the flow path due to \(T\) and \(P\):

\[
q_{T} = \frac{-1/V_{Qtz}}{\frac{\partial C_{Qtz}}{\partial x} + \frac{\partial C_{Qtz}}{\partial T}}
\]

\[21\]

in which \(V_{Qtz}\) is the molar volume of quartz and the coordinate direction \(x\) increases in, and is parallel to, the direction of flow. The \(\partial C_{Qtz}/\partial T\) and \(\partial C_{Qtz}/\partial P\) terms can be calculated using the known solubility of quartz (Figure 6(b)), whereas estimation of \(\partial T/\partial x\) and \(\partial P/\partial x\) requires some knowledge of thermal and baric gradients in the direction of flow. Since quartz solubility varies more strongly with \(T\) than with \(P\) along typical geotherms (Figure 6(b)), the \(\partial C_{Qtz}/\partial T\) term generally dominates \(\partial C_{Qtz}/\partial P\). The calculations do not account for kinetic effects. Nonetheless, in quartz-saturated rock sequences at metamorphic temperatures, concentration gradients in kinetically limited systems will still tend to approach local equilibrium gradients, even if the absolute concentration values depart from equilibrium (Ague, 1998). Equation [21] is inadequate, however, for shallow hydrothermal systems with high flow rates at relatively low \(T\) (Boltion et al., 1999).

Enormous fluxes on the order of \(10^{6} \text{ mol m}^{-2}\) imply that a column of fluid \(-1000 \text{ km}\) long flowed across each square meter of vein cross section! A similar flux would be required to dissolve large amounts of quartz out of a rock, but here, the fluid would have to flow in a direction of increasing \(T\) (‘up-\(T\)’ flow; Feehan and Brandon, 1999; Selverstone et al., 1991). The fluxes are large because changes in aqueous silica concentration along typical crustal geotherms are small. However, concentration gradients could be much steeper if quartz solubility drops due to decreases in water activity (Figure 6(c); Newton and Manning, 2000a; Walther and Orville, 1983). For example, local decreases in water activity due to increased fluid \(CO_{2}\) content near marbles could dramatically lower quartz solubility and, thus, produce quartz veins with a much lower flux than predicted by eqn [21]. In addition, quartz veins can form by diffusion-dominated processes that require little or no fluid flow (Section 4.6.9.3.1, in the succeeding text).

The advective treatment for quartz veins can be extended to other types of metasomatic reactions. For example, alkali metasomatism is possible if a large amount of fluid flow occurs along gradients in \(T\) and \(P\) (e.g., Ague, 1994b, 1997a; Dipple and Ferry, 1992a; Orville, 1962). Total concentrations of potassium increase and sodium decrease with increasing \(T\) for chlorine-bearing fluids in typical quartzofeldspathic and micaceous rocks (Figure 16; \(P\) effects are smaller). Consequently, up-\(T\) fluid flow will tend to destroy micas and/or potassium feldspars so as to remove potassium from the rock and, at the same time, produce a sodium-bearing phase, like plagioclase, and add sodium (\textit{Na metasomatism}). Down-\(T\) flow will do the opposite, favoring the growth of potassium-rich phases and destroying sodium-rich ones (\textit{K metasomatism}).

The expression describing the steady-state advection and reaction is similar to eqn [21] (Dipple and Ferry, 1992a):

\[
d_{T} = \frac{n_{Na}}{C_{Na,ag} \frac{\partial C_{Na,ag}}{\partial T} + C_{Na,ag} \frac{\partial P}{\partial T}}
\]

\[22\]

in which \(n_{Na}\) is the total moles of sodium produced (\(+)\) or consumed (\(-\)) per unit volume of rock. An analogous expression can be written for potassium. As shown in Figure 16, the concentrations of sodium and potassium increase and \(\partial C_{Na,ag}/\partial T\) changes as the total amount of chlorine in the fluid increases. Thus, chlorine molality must be known in order to evaluate the denominator of the expression. Furthermore, an unaltered starting rock or \textit{protolith} composition is needed so that sodium gains or losses due to alteration can be quantified to provide an estimate for the numerator. These metasomatic gains and losses are evaluated using mass balance methods (e.g., Ague, 1994a; Grant, 1986; Gresens, 1967; Philpotts and Ague, 2009). For typical total chlorine molalities of \(\sim 1 \text{ molal}\) and reasonable estimates for \(T\) and \(P\) gradients in the direction of flow, the time-integrated fluxes needed to cause alkali metasomatism are \(\sim 10^{5} \text{ m}^{3} \text{ m}^{-2} \text{ km}^{-1}\) (Ague, 1997a; Dipple and Ferry, 1992a; Ferry and Dipple, 1991). These fluxes are substantially smaller than those required to make quartz veins by advective flow (eqn [20]). Of course, metasomatism involving other elements that are transported effectively in chlorine-bearing fluids, including calcium, magnesium, and iron, can also be treated using eqn [22]. Metal leaching due to reaction with \textit{H}\textsuperscript{+} or \textit{HCl} (\textit{hydrogen metasomatism}) is generally possible only if fluxes are well in excess of \(10^{5} \text{ m}^{3} \text{ m}^{-2}\) due to the small concentrations of hydrogen species in typical fluids (e.g., \textit{HCl} + albite = 0.5 kyanite + 2.5 quartz + NaCl\textsuperscript{+} + 0.5H\textsubscript{2}O; see Ague, 1994b; Yardley, 1986).
Reactions involving H$_2$O–CO$_2$ fluids in metacarbonate rocks (mixed volatile reactions) are invaluable for assessing fluid fluxes and mass transfer processes. Common prograde reactions release CO$_2$, so fluids in closed or nearly closed systems should get richer in CO$_2$ during heating (Greenwood, 1975). In many metasedimentary sequences, however, reactions proceeded at relatively low X$_{CO2}$, implying that H$_2$O was also being added to the rocks (e.g., New England, United States; see Auge, 2002; Baumgartner and Ferry, 1991; Ferry, 1992, 1994a, 1994b; Hewitt, 1973). Input of external H$_2$O-bearing fluids, such as those derived from dehydrating schists or degassing magmas, can drive many prograde reactions (Figure 17(a); Ague and Rye, 1999; Hewitt, 1973). This type of infiltration has been treated quantitatively for advection-dominated systems (e.g., Ague and Rye, 1999; Dipple and Ferry, 1992a; Evans and Bickle, 1999; Hewitt, 1996) and for systems in which hydrodynamic dispersion is important (Ague, 2000, 2002; Ague and Rye, 1999).

Prograde reaction and CO$_2$ release can also occur, however, if fluids flow along gradients in T and P, as pointed out by Baumgartner and Ferry (1991). For a simple H$_2$O–CO$_2$ fluid, the analog of eqns [21] and [22] for mixed volatile reactions can be written as (Baumgartner and Ferry, 1991; Ferry, 1992, 1994a,b; Léger and Ferry, 1993)

$$q_{in} = \frac{V_f (n_i - X_i (n_{CO2} + n_{H2O}))}{(\frac{\partial n_i}{\partial T} + \frac{\partial n_i}{\partial P})}$$

[23]

in which $V_f$ is the molar volume of the fluid, $i$ is either CO$_2$ or H$_2$O, and $n_i$ is the total moles of $i$ produced (+) or consumed (−) per unit volume rock. The expression can be evaluated given the estimates for $P$, $T$, fluid composition, total volatile production/consumption, and gradients in $T$ and $P$ along the flow path. Volatile production/consumption is typically quantified using reaction progress methods (Brimhall, 1979; Ferry, 1983). For many common reactions proceeding under water-rich conditions, eqn [23] requires that prograde reaction and CO$_2$ release be driven by up-T fluid flow (Baumgartner and Ferry, 1991). For this case, fluid should become progressively more CO$_2$-rich along regional up-T flow paths; down-T fluid flow, by contrast, would tend to drive retrogression and remove CO$_2$ from the fluid (Figure 17(b)). Fluid salt content will also influence reaction progress along flow paths (e.g., Ferry and Gottschalk, 2000; Heinrich et al., 2004).

4.6.9 Examples of Mass and Heat Transfer

Bickle and McKenzie (1987) identified three broad crustal mass and heat transport regimes. In the first, fluid flow is limited, and chemical transport by diffusion and heat transport by conduction prevail. In the second, fluid fluxes are large enough so that advection of mass by fluid flow dominates diffusive transport. However, because conduction is relatively efficient, heat conduction through the rock still dominates heat advection by the fluid. Many deep-crustal systems are inferred to have formed in this regime (e.g., Manning and Ingebritsen, 1999). In the third regime, fluxes are very large, and both chemical and heat transport are predominantly by fluid flow. In addition to these three categories, hybrid modes of transport are possible. For example, regional-scale fluid flow along fractures can be coupled to local-scale diffusion to and from the wall rock adjacent to the fractures. The mass and heat transfer literature is vast and cannot be reviewed fully here; thus, the following sections explore some selected examples that illustrate a representative spectrum of processes.

4.6.9.1 Regional Devolatilization and Directions of Fluid Motion

4.6.9.1.1 Shallow crustal levels

The processes of metamorphic volatile release and the directions of fluid motion are basic questions in deep-crustal petrology (Figure 18). Recirculation of fluid by convection

![Figure 17](image_url) Two ways to drive CO$_2$ loss or gain for a common mineral assemblage in metacarbonate rocks (0.7 GPa). (a) Fluid composition I is more water-rich than the equilibrium fluid composition (solid line) at 520°C and is in the stability field of the reaction products tremolite and calcite. Input of this fluid into a metacarbonate layer would thus drive prograde reaction and CO$_2$ loss. Input of fluid II would drive retrograde CO$_2$ gain. Fluid could be input by, for example, direct flow through a metacarbonate layer or diffusion/mechanical dispersion across lithologic contacts or vein margins. (b) Fluid flowing in a direction of increasing temperature (up-T flow) at or near local equilibrium with the assemblage dolomite + quartz + tremolite + calcite must get progressively richer in CO$_2$; it does so by driving prograde reaction and CO$_2$ release from the rock. Down-T flow would drive retrograde CO$_2$ gain. Computed following Auge (2000b).
Fluid Flow in the Deep Crust

(multipass flow; e.g., Etheridge et al., 1983) is widely recognized in shallow hydrothermal systems (Norton and Taylor, 1979). However, the conventional wisdom is that permeability is too small at deeper levels to allow the downward penetration of fluid necessary for convection (e.g., England and Thompson, 1984; Hanson, 1997; Manning and Ingebritsen, 1999; Walther and Orville, 1982). Nonetheless, studies of active mountain belts in New Zealand and Pakistan have shown that shallow fluids can penetrate to at least midcrustal levels near the brittle–ductile transition (e.g., Koons and Craw, 1991; Poage et al., 2000; Templeton et al., 1998). For example, fluid inclusion and stable isotopic systematics in Nanga Parbat, Pakistan, led Poage et al. (2000) to conclude that meteoric fluids penetrate downward to depths of ~10 km, where they mix with CO₂-rich fluids of metamorphic origin in the rapidly uplifting core of the mountain belt. Overall fluid fluxes, however, are inferred to be small, except in fault zones. Wickham and Taylor (1990) concluded that massive penetration of marine fluid to depths of at least 10–12 km resulted in widespread homogenization of stable isotope ratios in the Hercynian basement of the Pyrenees. Convection is also one possible explanation for midcrustal thermal anomalies preserved within the rock record in New Hampshire (Chamberlain and Rumble, 1989; Section 4.6.9.6).

The Mt. Isa Inlier, north Queensland, Australia, contains some of the largest metasomatic provinces exposed on the planet. Here, a complex and long-lived Paleo- to Mesoproterozoic metamorphic and fluid flow history produced widespread scapolitization, albitionization (Na–Ca metasomatism), and ore deposition (e.g., Oliver et al., 1990, 2008; Rubenach, 2005; Rubenach and Lewdhaitie, 2002). Although mass transfer affected the rock mass regionally at length scales on the order of 10–100 km, much of the most intense metasomatic activity occurred in and around shear zones, fractures, boudins, and breccia zones. Magmatic fluids, regional devolatilization, inflow from shallower crustal levels, and high-CI, high-S fluids sourced from metamorphosed evaporite-bearing dolomitic rocks were all likely important at various times in the region’s evolution.

The Mt. Isa rocks underwent fluid–rock reactions in the upper crust (<~0.4 GPa), considerably shallower than most of the other examples discussed in this chapter. Hydrologic processes at these levels likely differ considerably from those in the deeper crust. For example, Oliver et al. (1990) posit that dilatancy (or seismic) pumping during deformation was able to circulate fluids repeatedly through the Mary Kathleen Fold Belt at crustal levels around the hydrostatic–lithostatic fluid pressure transition (see Cox and Etheridge, 1989; Sibson et al., 1975). In this scenario, fractures and other kinds of pore space are created by rising tectonic shear stresses in zones of active deformation, producing low-pressure zones into which fluid flows. Under appropriate circumstances, this process can drive flow downward or sideways. The fluid inflow causes fluid pressures to rise, weakening the rock, and ultimately leading to failure (in many cases seismogenic). Collapse of pore space following deformation then drives fluid rapidly upward. In this way, circulation takes place and large fluid fluxes are generated due to repeated deformational-fluid flow cycles. The absence of Mt. Isa-type regional metasomatism in deeper rocks is important evidence that this kind of fluid circulation is probably limited to upper-crustal metamorphic environments.

4.6.9.1.2 Deeper levels

Fluid fluxes and flow directions at deeper-crustal levels continue to be the focus of vigorous research. The single pass flow model holds that fluids generated during devolatilization move upward toward the surface (e.g., Walther and Orville, 1982). Modeling of simple systems, such as fluid flow during thermal relaxation and exhumation of tectonically thickened crust, indicates a strong upward component of flow (Figure 19). Substantial prograde devolatilization occurs in the lower thrust plate; these upward-migrating fluids can produce retrogression in the base of the upper plate, which undergoes a period of cooling after thrust emplacement. The simple models shown in Figure 19 do not include the important effects of compaction (Connolly, 1997, 2010). In general, compaction will tend to reinforce the upward component of flow. Notably, large-scale convective circulation is not predicted at middle and lower crustal levels. In the simple model shown, this is due largely to the fact that devolatilization increases fluid pressures, driving fluid upward and out of the system. Moreover, when retrograde hydration in the base of the upper plate occurs, it can act to pull fluid upward. Downward motion associated with topographically driven flow is predicted at shallow crustal levels where permeability is higher (Figure 19b: Garven and Freeze, 1984a, 1984b). Small downward fluxes at shallower levels may also be caused by retrograde hydration that draws fluid downward (Lyubetskaya and Ague, 2009) and may help explain the downward flow observed in the crystalline basement in Central Europe (Stober and Bucher, 2004) and the Transcaucassian region (Yakovlev, 1993).

Of course, flow can also have significant nonvertical components, particularly in the presence of permeability anisotropy, barriers to flow, conduits for flow, fluid sinks, and other heterogeneities (cf. Connolly, 2010; Hanson, 1997; Lyubetskaya and Ague, 2009). For example, permeability anisotropy due to layering and foliations can be considerable. Fluids can be constrained to follow flat-lying flow paths if layering is subhorizontal, given
that permeability can be an order of magnitude or more greater parallel to layering than perpendicular to it (Figures 5 and 18; Ingebritsen and Manning, 1999). Moreover, barriers to flow, such as low-permeability metamorphic aquicludes (Ferry, 1987), can divert upward-migrating fluids horizontally at regional scales (Lyubetskaya and Ague, 2009). Although regional deep-crustal convection seems unlikely given the present knowledge, it has been postulated that smaller-scale, local convection could develop (e.g., Etheridge et al., 1983, 1984; Yardley, 1986). Wing and Ferry (2002, 2007) used a method akin to those developed for tracing ocean circulation patterns (Lee and Veronis, 1989) to estimate regional time-integrated fluid fluxes and flow directions based on a three-dimensional inversion of reaction progress, $\delta^{18}O$, and $\delta^{13}C$ data for metamorphic rocks in Vermont, United States. Their results suggest that the fluid flow was highly complex locally and included

![Figure 19](image-url)
both upward and downward regimes. On the regional scale, however, flow was dominantly upward and parallel to regional lithologic layering.

A fundamental question regarding flow directions is whether they are in a direction of increasing temperature (up $T$) or decreasing temperature (down $T$). This distinction is important because the two flow regimes produce considerably different chemical and isotopic shifts in rocks (Section 4.6.8). For example, up-$T$ flow can drive decarbonation reactions, produce sodic–calcic metasomatism, dissolve silica, and decrease rock ${\delta}^{18}\text{O}$. Down-$T$ flow will promote carbonation, potassic metasomatism, silica precipitation, and increases in ${\delta}^{18}\text{O}$. In the absence of magmatism, upward flow will generally be down $T$ (Figure 19(b)). Subhorizontal flow could potentially be either down $T$ or up $T$, depending on regional thermal structure. However, numerical models indicate that, while subhorizontal flow is expected in the presence of appropriate permeability heterogeneities, it will generally be down $T$ during prograde heating. Fluid production during devolatilization will act to increase fluid pressures. Consequently, as devolatilization proceeds in the hotter cores of orogens, it is unlikely that large fluxes of cooler fluids will flow sideways and up $T$ into these regions of fluid production (Hanson, 1997; Lyubetskaya and Ague, 2009).

It is still possible, however, that large up-$T$ fluxes may develop at regional scales. Magmas that are emplaced at mid- to deep-crustal levels can produce long-lived inverted geotherms. If devolatilization fluids generated deeper in the metamorphic pile flow upward into these perturbed thermal zones, then they will move up $T$ beneath (and on the flanks of) the intrusions (Lyubetskaya and Ague, 2010). Another possible up-$T$ flow scenario is if protracted underthrusting gives rise to long-lived inverted geotherms at the base of the overthrust plate or top of the underthrust plate. Deeply generated fluids would then flow upward and up $T$ into the thrust zone (e.g., Selverstone et al., 1991). Clearly, much field, experimental, and modeling work lies ahead to determine fluid flow directions in the deep crust.

### 4.6.9.2 Regional Fluid Fluxes

Middle- and lower-crustal fluid fluxes likely vary by several orders of magnitude in natural geologic environments. Time-integrated fluid fluxes for simple single pass flow constrained by the thickness of the metamorphic pile undergoing devolatilization are straightforward to quantify. Consider a crustal control volume having a uniform cross-sectional area $A$ = 1 m$^2$, length $L_c$, and constant, fluid-filled porosity. The mass of fluid produced by devolatilization per unit initial volume of rock ($f_{\text{inv}}$) is

$$f_{\text{inv}} = f_m \rho_s (1 - \phi)$$  \[24\]

in which $\rho_s$ is the density of the solid (not including porosity) and $f_m$ is the mass of fluid released per unit initial mass solid. If all the fluid produced flows unidirectionally out of the top of the column and if small volume changes due to devolatilization reactions are ignored, then the time-integrated fluid flux across the top surface of the column is

$$q_{\text{fit}} = f_m L_c \rho_f$$  \[25\]

in which $\rho_f$ is the density of the fluid exiting the column. For example, a metasedimentary pile (or degassing magma) loses 2.25 wt% water ($f_m$~0.025), and the densities of fluid and solid are 950 and 2800 kg m$^{-3}$, respectively. Taking a representative crustal-scale column 15 km long having $\phi$ = 0.001, then $q_{\text{fit}}$ is ~1000 m$^3$ m$^{-2}$ (Figure 20). These calculations are insensitive to reasonable variations in porosity. It is worth emphasizing that this large value means that a column of fluid 1 km long passes over each meter square of rock area at the top of the column, sufficient to displace an oxygen isotope front some 600 m (Section 4.6.7). Even the loss of just 1 wt% would...
water from a 10 km long column produces nearly 300 m$^3$ m$^{-2}$; longer columns and larger amounts of devolatilization generate correspondingly larger fluxes (Figure 20). Small regional fluxes less than \( \sim 100 \text{ m}^3 \text{ m}^{-2} \) would be expected only if the rocks involved in orogenesis were already dry to begin with (e.g., high-grade gneisses or metagneous rocks).

These simple calculations lead to the inescapable conclusion that considerable fluid fluxes will accompany regional devolatilization in orogenic belts. Pervasive fluxes on the order of 500–1000 m$^3$ m$^{-2}$ are clearly consistent with the range of estimates from natural settings shown in Figure 21. For example, carbonate-bearing metasedimentary rocks in the Acadian orogen of New England, United States, preserve a valuable record of fluid–rock interaction (Baumgartner and Ferry, 1991, Ferry, 1992, 1994a, 1994b; Léger and Ferry, 1993; Wing and Ferry, 2002, 2007). Estimated time-integrated fluid fluxes in the Waits River Formation, Vermont, increase from \( \sim 10^2 \text{ m}^3 \text{ m}^{-2} \) in the greenschist facies to \( \sim 7 \times 10^3 \text{ m}^3 \text{ m}^{-2} \) in the amphibolite facies (Figure 21), consistent with the ranges calculated in Figures 3 and 20. Fluid fluxes were sufficient to produce C and O isotopic shifts and variable degrees of alkali metasomatism.

This regional flow was part of a complex hydrologic system in which the prograde release of CO$_2$ and H$_2$O was critically dependent on local fluid–rock interactions between intercalated metacarbonate, metapelite, and metasandstone layers. As discussed earlier, infiltration of fluid with lower XCO$_2$ than the equilibrium value for a given rock can drive reaction (Figure 17(a)). For example, H$_2$O derived from dehydrating metapelites that infiltrates into metacarbonate layers across lithologic contacts or vein margins (selvages) by hydrodynamic dispersion (Ague, 2000; Ague and Rye, 1999; Hewitt, 1973) or by advection (Ague and Rye, 1999; Evans and Bickle, 1999) can drive substantial prograde CO$_2$ loss (Figure 17(a)). In this way, prograde dehydration and decarbonation are coupled. Field tests show that length scales for hydrodynamic transport across layers range from the decimeter scale to tens of meters (Ague, 2003; Bickle et al., 1997; Ferry, 2008; Penniston-Dorland and Ferry, 2006). Degasging magmas are another significant source of H$_2$O that can, at least in part, account for water-rich diopside zone conditions that drove prograde CO$_2$ loss (Figure 17(a); Ague, 2002; Ague and Rye, 1999; Léger and Ferry, 1993; Palin, 1992; Wing and Ferry, 2007).

Fluid fluxes will likely vary widely across metamorphic belts, even within the same facies or index mineral zone. Modeling predicts that time-integrated fluxes will tend to be higher through rocks in the upper parts of metamorphic sequences, as they overlie longer integrated length scales of devolatilization (Figure 19(c)). Large fluxes are predicted to develop at deeper levels as well, depending on many geologic factors, including regional thermal structure, extent of devolatilization, and flow focusing. For example, Figure 19(c) predicts that time-integrated fluid fluxes could vary from a few 100 m$^3$ m$^{-2}$ to well over 1000 m$^3$ m$^{-2}$, all within the kyanite zone of regional metamorphism. The most vigorous circulation in Figure 19 is generated by the topographically driven flow of surficial fluids in the higher-permeability, shallower parts of the crust (\( \sim 10–15 \text{ km} \)), producing time-integrated fluxes of \( \sim 10^4 \text{ m}^3 \text{ m}^{-2} \). Within this region, shallow fluids will mix with deeper metamorphic basement fluids produced by devolatilization; this mixing may have important consequences for ore deposition. These results are, of course, specific to the model’s initial and boundary conditions but still illustrate general levels of variability to be expected in collisional orogens.

### 4.6.9.3 Channelized Flow

Regional time-integrated fluid fluxes of \( \sim 10^2–10^3 \text{ m}^3 \text{ m}^{-2} \) should be commonplace during crustal-scale devolatilization. Furthermore, a survey of the literature shows that structural features that focus flow, including veins, fold hinges, permeable layers, and ductile shear zones, may transfer significantly greater fluxes of fluid, ranging from \( \sim 10^3 \text{ m}^3 \text{ m}^{-2} \) to in excess of \( 10^5 \text{ m}^3 \text{ m}^{-2} \) (Figure 21). These fluxes are large enough to cause significant isotopic shifts and mass transfer of rock-forming elements. If the focused flow conduits deprive other areas of the rock mass of fluid, then regionally averaged fluxes could, of course, be less than \( \sim 10^4 \text{ m}^3 \text{ m}^{-2} \).

#### 4.6.9.3.1 Fractures, veins, and shear zones

Rock failure caused by, for example, hydrofracture or tectonic stress, will create fractures that increase rock permeability (eqn [4]) and focus flow. Veins (mineralized fractures) can be present at all levels of the crust and in the high-pressure and ultrahigh-pressure rocks of subduction zones (see succeeding text). They are unambiguous indicators of mass transfer. The nature and scale of mass transfer, however, vary strongly, depending on the vein-forming process. Vein minerals may be precipitated from large-scale fluid flow through regional fracture systems, local diffusion of mass to (and from) fractures through an essentially stagnant pore fluid, and local-scale fluid flow from wall rocks to fractures (e.g., Ague, 1994b, 1997b; Ferry and Dipple, 1991; Fisher and Brantley, 1992; Oliver and Bons, 2001; Oliver et al., 1990; Walther and Orville, 1982; Whitney et al., 1996; Widmer and Thompson, 2001; Yardley, 1975, 1986; Yardley and Bottrell, 1992). The fluid fluxes required to precipitate veins by regional flow are large, but local formation by diffusional mass transfer may occur with little or no flow (Figure 22). Consequently, vein formation mechanisms must be assessed before any conclusions about fluid fluxes can be drawn.

Veins can make up a significant portion of outcrops. For example, in the chlorite through stauroilite Barrovian zones north of Stonehaven, Scotland, veins occupy \( \sim 1–18 \text{ vol}\% \) of the rock mass; 5–15% is typical (Masters and Ague, 2005). The lowest values are measured in quartzofeldspathic layers, the highest in metapelitic ones. Significant fracturing and veining also occurred during Barrovian-style metamorphism of the Wepawaug Schist, Connecticut. Historically, it is interesting to note that these were probably the first metamorphic veins to be described in a North American scientific publication (Silliman, 1820). Here, vein abundance increases from a few vol\% in the chlorite zone to 20–30% in the amphibolite facies (Ague, 1994b). In their study of veining in metapelitic rocks of the Waits River Formation, Vermont, Penniston-Dorland and Ferry (2008) measured 4.5% veins in a chlorite zone outcrop and over 12% in a kyanite zone outcrop. In the Otago Schist,
New Zealand, vein proportions increase from a few percent or less in the lowest-grade rocks to as much as 30% in the greenschist facies rocks (Breeding and Ague, 2002).

The source of vein mass is critical to evaluate in order to assess fluid fluxes, but relatively few studies have quantified the proportions of internally and externally derived vein mass. Those that do commonly conclude that a significant proportion of the vein mass was externally derived and was precipitated from through-going fluids. For example, in the Wepawaug Schist, thin section, outcrop-scale, and regional-scale analyses indicate that ~30% of the mass in the average amphibolite facies quartz vein was externally derived; in some cases, the proportion

Figure 21  Selection of time-integrated fluid fluxes from the literature. The average regional, pervasive flow-dominated flux of $10^{2.7\pm0.5}$ $m^3/(m^2\cdot s)$ denoted with diagonal ruled bar (computed using geometric mean). Data sources as follows: (a) Breeding and Ague (2002); (b) Ferry (1992); (c) Ague (1994b); (d) Oliver et al. (1998); (e) Penniston-Dorland and Ferry (2008); (f) Chamberlain and Rumble (1989). Range computed using average flux of $1.5\times10^3 m^3/m^2/s$ for $10^5$ and $10^6$ years. (g) Bickle (1992); (h) Selverstone et al. (1991); (i) Penniston-Dorland and Ferry (2008); (j) Ague (1994b); (k) Ague (2003); (l) Ague (1997a); (m) Dipple and Ferry (1992a); (n) Lyubetskaya and Ague (2009); (o) Ferry (1992), Léger and Ferry (1993), and Wing and Ferry (2007); (p) Skelton et al. (1995); (q) Walther and Orville (1982) and Walther (1990). Range computed using total timescales of fluid flow of $10^5$ and $10^7$ years. (r) Hanson (1997) and Lyubetskaya and Ague (2009); (s) Evans and Bickle (1999); (t) Schmidt and Poli (see Chapter 4.19).
is as high as ~60% (Ague, 1994b, 2011). The remainder was derived from silica-depleted selvage zones adjacent to the veins. Penniston-Dorland and Ferry (2008) found even larger proportions; their estimates for externally derived vein mass exceed 90%.

If quartz precipitation occurred largely in response to decreases in pressure and temperature along regional flow paths, which seems likely, then the necessary time-integrated fluid fluxes are enormous (eqn [21]; e.g., Yardley, 1986; Walther, 1990; Ferry and Dipple, 1991). Estimated \( q_{\text{TI}} \) values are \( \approx 2.8 \times 10^7 \, \text{m}^2 \, \text{m}^{-2} \) for the average amphibolite facies vein in the Wepawaug (Ague, 1994b) and \( 4-9 \times 10^7 \, \text{m}^2 \, \text{m}^{-2} \) for the Waits River Formation veins (Penniston-Dorland and Ferry, 2008). Geochemical interactions between infiltrating fluids and adjacent wall rocks were facilitated by diffusion with some contributions from advection, producing chemically and isotopically altered vein selvages (Figure 22(b)).

The presence of both internally and externally derived vein mass gives valuable clues regarding processes of vein formation. In the crack–seal vein formation model of Ramsay (1980), cracks open during deformation and then are sealed by mineral precipitation. The process is repeated many times to build up typical veins. Fluid inclusion evidence suggests that the initial fluid pressure drop upon fracturing can be as great as ~0.1 GPa in accretionary prism settings (Vrolijk, 1987); such large drops are likely to be highly transient and short-lived (Fisher and Brantley, 1992). For quartz veins that contain
both internally and externally derived mass, it is likely that deformation created fractures that were zones of elevated permeability and that channelized fluid flow. Some precipitation of silica (or other vein-forming constituents) occurred as the fluids flowed down P and T gradients in the fractures. This flow was accompanied and/or followed by fracture sealing due to local diffusional transport of silica from wall rocks to fractures, producing altered, silica-depleted selvages marginal to the veins. The chemical potential gradients necessary to drive diffusion could have arisen due to gradients in a number of variables, including strain energy, surface free energy, and fluid pressure (e.g., Elias and Hajash, 1992; Fisher and Brantley, 1992; Yardley, 1975). This crack flow seal process would be repeated many times to build up large quartz veins (Figure 22(b)). Crack–seal textures (Ramsay, 1980) are commonly preserved and attest to multiple episodes of fracture opening and healing (see Oliver and Bons, 2001; and references therein).

Not all veins are regional flow conduits (Figure 22(a)); some may represent essentially closed-system fracture infillings developed during deformation (e.g., Henry et al., 1996; Ramsay, 1980; Verlaguet et al., 2011; Yardley and Bottrell, 1992). In such cases, all vein mass must be derived from the local wall rocks. Nonetheless, to the author’s knowledge, very few studies attempt to demonstrate this quantitatively using mass balance, even though some (e.g., Verlaguet et al., 2011) assume a closed-system behavior except for H2O. Isotopic studies are, however, more numerous. For example, Yardley and Bottrell (1992) found that oxygen isotope ratios for quartz in veins and their enclosing wall rocks in the Connenara Schists (Ireland) were essentially identical, suggesting limited fluid–rock interaction and local derivation of vein mass.

An ambiguity, however, is that infiltrating fluids may have altered the isotopic ratios of wall rock quartz to the point that they were indistinguishable from the veins. This problem can be addressed by a study of isotopic zonation within refractory minerals, such as garnet (e.g., Page et al., 2010). If such crystals grow during infiltration, then they can provide an invaluable record of the isotopic evolution of the fluid, even when other minerals have largely equilibrated with vein fluids (see Chapter 4.7). For example, van Haren et al. (1996) found that garnet rims were as much as ~2% heavier than garnet cores in an alteration selvage adjacent to an amphibolite facies vein cutting metapelites. They concluded that the garnets record progressive increases in the δ18O of the selvage resulting from isotopic exchange between the wall rock and large fluxes of regional devolatilization fluids that ascended through fractures (down-T flow will tend to partition the heavy oxygen into the rock). Garnets outside the selvages contain significantly less zonation, indicating smaller degrees of fluid–rock reaction away from the veins (e.g., Kohn et al., 1993).

Shear zones can be loci of extensive focused fluid flow, metasomatism, and mass transfer-related volume changes (e.g., Dipple and Ferry, 1992a; Dipple and Wintsch, 1990; Konrad-Schmolke et al., 2011; O’Hara, 1988; Ring, 1999; Selverstone et al., 1991). In their survey of ductile shear zones, Dipple and Ferry (1992a) concluded that time-integrated fluid fluxes of ~2 × 10^4 m^3 m^-2 attended down-T flow, leading to considerable K gain and other major element metasomatism. Selverstone et al. (1991) documented extreme metasomatism in a shear zone from the Tauern Window, Austria. Granodiorite host rock was converted to highly aluminous schist as a result of fluid–rock interaction in the shear zone; time-integrated fluid fluxes were ~10^5 m^3 m^-2. In the Bergen Arcs, Norway, flow along shear zones, veins, and infiltration fronts facilitated conversion of metastable deep-crustal granulite facies rocks to eclogite facies assemblages (Figure 8; Austheim, 1990).

4.6.9.3.2 Lithologic contacts and layer-parallel flow
Large time-integrated fluid fluxes are predicted and observed for regional devolatilization. Nonetheless, some rocks preserve evidence for considerably less advection. For example, Bickle et al. (1997) studied greenschist facies fluid infiltration from metapelitic rock into metacarbonate rock across lithologic contacts in the Waterville Formation, Maine. They estimated time-integrated fluid fluxes of only ~3.2 m^3 m^-2. Fluxes from metapelites into marbles recorded in the amphibolite facies on Naxos, Greece, were similarly small, ranging from 0.2 to 1.0 m^3 m^-2 (Bickle and Baker, 1990). These small values can be reconciled with the expectation of larger regional devolatilization fluxes if the regional flow was predominantly layer parallel, such that cross-layer components were small. On Naxos, the marbles probably had very low permeability, resulting in the bulk of the flow being channeled into the metapelitic layers (e.g., Figure 5). Oliver et al. (1998) quantify fluxes for an example of regional focusing into metapelitic layers. Fluids flowed up-T over 20 km length scales in the vicinity of the Kanmantoo ore deposit, Australia, achieving large time-integrated fluid fluxes of ~10^6 m^3 m^-2, which led to substantial chemical and oxygen isotopic metasomatism. Although flow channelized along layers and lithologic contacts has been widely recognized in many studies (see review in Oliver, 1996), the number of quantitative estimates of time-integrated fluid fluxes for cross-layer and layer-parallel flow components remains surprisingly modest.

4.6.9.3.3 Flow channelization in subduction zones
Subduction zone fluids and mass transfer are very large topics that are examined in depth in Chapters 4.9, 4.19, and 4.20; nonetheless, it is useful to discuss some aspects of the fluid flow here. A basic constraint is that the time-integrated fluid flux at the top of the slab, assuming vertical flow, will be ~3 × 10^7 m^3 m^-2 (Zack and John, 2007; see Chapter 4.19). This flux is considerable – sufficient to transport an oxygen isotopic front some 180 m – but is still smaller than expected for devolatilization in some other settings, such as collisional orogens (Figure 19(c)).

As seen in the previous examples, however, focusing of fluid will produce larger fluxes in and around flow conduits. Veins are one means to focus flow; they have been documented widely in diverse exhumed subduction complexes, including the Catalina Schist, California (Bebout and Barton, 1989), the Tianshan subduction complex, China (Gao et al., 2007; John et al., 2008), and Guatemala (Simons et al., 2010). The flow direction is also critical. A major, as yet unresolved question is, do fluids always flow vertically up out of the slab, or can they be channeled along the subduction zone décollement? If channeled, then larger fluxes could be focused along the slab–mantle interface. Studies of subduction zone mélanges are critical in this regard. These mélanges typically consist of metamorphosed igneous (predominantly mafic and ultramafic)
and/or sedimentary rocks set in a metasedimentary or ultramafic matrix. In many cases, field evidence indicates that they probably represent the interface between the downgoing lithosphere and the overlying mantle wedge (see Chapter 4.20). Consequently, mélanges will hold valuable clues about fluid flow in dynamic subduction environments.

In view of the critical role subduction plays in arc magmatism and global element cycling, the quantities and directions of fluid flow within subducted crust remain the subjects of vigorous investigation. Different workers, however, have come to markedly different conclusions regarding the nature and extent of subduction-related fluid flow. Field studies of stable isotope systematics (e.g., Bebout and Barton, 1989, 1993) and trace element mobility (e.g., Cruz-Uribe et al., 2010; Sorensen and Grossman, 1989) provide strong evidence for regional, kilometer-scale fluid migration during Mesozoic subduction in the Cordillera (CA, USA).

By contrast, diverse evidence from the Cycladic Archipelago (Greece) and the Alps indicates that subduction during Alpine orogenesis may have involved limited fluid flow and fluid–rock interaction (e.g., Barnicoat and Cartwright, 1995; Bröcker et al., 1993; Ganor et al., 1996; Getty and Selverstone, 1994; Philippot and Selverstone, 1991; Putlitz et al., 2000). For example, little evidence has been found for fluid–rock interactions during subduction on the Cycladic island of Naxos; the classic metamorphic sequence there formed during a later Barrovian-style overprint of original high-P, low-T assemblages (Bickle and Baker, 1990; Rye et al., 1976). Putlitz et al. (2000) found no evidence favoring the large-scale release of fluids during high-P, low-T metamorphism of subducted oceanic crust based on O and H isotope studies of metabasalts and metagabbros in the Cyclades.

One possible explanation for the comparatively low fluid fluxes seen in these regions is channelization of fluids into high-permeability structures during Alpine orogenesis, which led to strong spatial heterogeneity of flow. Fractures are one candidate for such channels, although regionally extensive vein systems have yet to be documented. Veins are present, but were not necessarily conduits for large fluxes; in fact, Philippot and Selverstone (1991) documented local-scale heterogeneities in fluid composition recorded by eclogitic veins, which they interpreted to reflect limited fluid flow.

Another, perhaps more likely, scenario for the low fluid fluxes is channelization of fluids into mélangé zones. Strong metasomatic interactions between the rims of metamorphosed igneous and sedimentary rocks and the surrounding mélangé matrix occurred in mélangé zones in both the California and Alpine/Cycladic settings, unequivocally demonstrating the presence of fluids (Bebout and Barton, 2002; Breeding et al., 2004b; Bröcker and Enders, 2001; Catlos and Sorensen, 2003; Dixon and Ridley, 1987; King et al., 2003; Miller et al., 2009; Putlitz et al., 2000). Metasomatic rinds on mafic blocks in ultramafic matrix at Syros, Greece, show clear enrichments of lithium and boron related to fluid infiltration during exhumation (Marschal et al., 2009). Nonetheless, the time-integrated fluid fluxes recorded by the block interiors are relatively small, probably <17 m^3 m^{-2} (Ague, 2007). However, the blocks are typically quite massive, in contrast to the highly foliated matrix. Thus, the blocks may have had much lower permeabilities than the matrix, such that the major flow was channelized into the matrix and concentrated on block margins. Numerical simulations show that order of magnitude flux contrasts may develop over length scales as short as decimeters in mélangé zones with high permeability contrasts (Figure 23). Of course, mélanges undergo extensive deformation, but the general process of flow diversion around low-permeability blocks will hold true regardless.

If the flux out of the top of the downgoing lithospheric column (~3 x 10^7 m^3 m^{-2}) travels mostly upward, then it will enter the hanging wall of the subduction zone. As subduction-related fluids will be generated on timescales on the order of 10^7–10^8 years, the total flux into the hanging wall will be much larger than that emanating from any one point at the top of the subducted crust. Peacock (1990) estimates fluxes will range from <10^{-4} to 10^{-3} m^3 m^{-2} year^{-1} during subduction, depending on the nature of the devolatilization reactions proceeding as a function of depth. Taking a conservative value of 10^{-4} m^3 m^{-2} year^{-1} and timescales of 10^7 and 10^8 years, the corresponding time-integrated fluid fluxes into the hanging wall are 10^5–10^6 m^3 m^{-2}. Of course, the flux at any given point along the subduction zone will be a complex function of thermal history, reaction progress, reaction kinetics, and other geologic factors. Nonetheless, this flux is critical to consider when evaluating fluid flow into accretionary prisms, mantle metasomatism, and the genesis of arc magmas. For example, Breeding and Ague (2002) estimated large regional time-integrated fluid fluxes of c. >10^4 m^3 m^{-2} for fracture-controlled flow into the Otago Schist accretionary prism, New Zealand, based on a mass balance analysis of silica addition to regional quartz vein sets. The fluid fluxes were large.

![Figure 23](image) Numerical model of fluid flow in mélange with large permeability contrasts. Mélange blocks (circles and ellipses) have low permeability relative to matrix. Flow is diverted around blocks, leading to concentrated zones of high flux on block margins. Fluxes can vary by orders of magnitude over meter or even decimeter scales. General direction of flow is upward. Modified from Ague JJ (2007) Models of permeability contrasts in subduction zone mélange: Implications for gradients in fluid fluxes, Syros and Tinos Islands, Greece. Chemical Geology 239: 217–227.
enough to produce Au mineralization in Otago and in accretionary environments elsewhere (e.g., Craw and Norris, 1991; Jia and Kerrich, 2000) and to provide a mechanism for the long-term bulk silica enrichment of the continents.

The evolving picture of fluid flow in subducted lithosphere suggests that channelization of fluid is common, such that conduits experience high fluxes and the surroundings are impoverished in fluid (e.g., Zack and John, 2007). However, many fundamental questions persist. Indeed, the fact remains that very few field-based estimates of time-integrated fluid fluxes are available for subduction zones. It is essential to clarify the fluid flow picture, since subduction of sediment and hydrothermally altered oceanic crust and mantle is the primary means by which reactive volatiles, including H₂O and CO₂, are returned to the deep earth, ultimately giving rise to arc magma genesis at ~100–150 km depth.

### 4.6.9.4 Channelization and Fluid Fluxes at the Regional Scale

As shown in Figure 21, the maximum large-scale fluxes are associated with areas of long-term regional flow channelization into fracture sets or with flow patterns generated around cooling intrusions. Fracture-controlled, outflow of fluids during regional metamorphism, metamorphic hot spot genesis (see Section 4.6.9.6), and devolatilization of subducted slabs beneath accretionary prisms can involve large-scale fluxes of ~10⁴ to >10⁵ m³ m⁻². Fluid flow toward cooling intrusions may also produce fluxes in this range, although examples to date are mostly from midcrustal levels (~<15 km depth). Large-scale focusing of flow is one way to produce regional time-integrated fluxes well in excess of 10⁴ m³ m⁻². For example, areal focusing of devolatilization fluids derived from underlying crust by a factor of ~10–20 could have produced the large fluxes recorded by the regional vein systems of the Wepawaug Schist (Ague, 1994b). Subduction can also generate large time-integrated fluid fluxes in the hanging wall, as the supply of fluid is continually replenished as new oceanic crust and sediment is fed into the subduction zone and undergoes devolatilization during burial (Nur and Walder, 1990). In addition, large fluxes could potentially be achieved by convective recycling of fluids or by the long-term circulation of fluids derived from near surface reservoirs into the deep crust. These latter two possibilities seem unlikely for the deep crust, given current understanding, but future research may prove otherwise.

### 4.6.9.5 Mass Transport by Fluids

Fluid flow through rocks will transport volatile species (e.g., H₂O and CO₂) and nonvolatile rock-forming and trace elements. Volatiles have received a tremendous amount of attention, but the geochemical behavior of the nonvolatile elements is also crucial to understanding. For example, Rh/Sm, Sm/Nd, and Lu/Hf isotopic dating of garnet is predicated on the immobility of these elements in crustal fluids. Fluid-driven, coupled dissolution–precipitation reactions and phosphorous mobility can cause major changes in the U–Th–Pb systematics of accessory minerals commonly used for dating, such as monazite (Section 4.6.6.3). The transport of rock-forming elements, such as alkali and alkaline earth metals and aluminum, can modify rock bulk chemistry and stabilize or destabilize key metamorphic index minerals. In subduction zones, release of these and other elements (including silicon) during devolatilization can produce silicification of the mantle wedge (e.g., Kesson and Ringwood, 1989) and exert profound controls on arc magma chemistry (Chapters 4.9, 4.19, and 4.20). Fluid–rock reaction leads to chemical and isotopic modification of rocks and minerals, providing an invaluable record of fluid flow histories that permits quantification of fluid fluxes (Sections 4.6.4–4.8). Furthermore, element transfer by fluids deep in mountain belts must play a considerable role in large-scale geochemical cycling and ore deposition; interactions between deep and shallow fluids remain an important research frontier.

It has long been understood that certain trace elements can be mobilized in crustal fluids. For example, the mobility of strontium has been quantitatively appreciated since the early days of Rb–Sr dating. Some soluble elements, like lithium, can be lost together with water and other volatiles during prograde heating (Qiu et al., 2011; Teng et al., 2007). Owing to their low concentrations in rocks, trace elements will tend to be more easily mobilized by infiltrating fluids than major elements. This is not true of HFSE, like zirconium, however, which tend to have extremely low concentrations in fluids (Section 4.6.5). The received wisdom has been that most rock-forming elements and HFSE are largely inert during orogenesis, but research over the past few decades has shown that a more diverse spectrum of geochemical behavior is possible.

Some of the most well-established examples of fluid-driven, mid- to deep-crustal mass transfer are found in and around veins, shear zones, or lithologic contacts. As shown in Figure 21, these features can act as flow conduits and carry large fluxes, which may exceed 10⁴ m³ m⁻² on a time-integrated basis. The large fluxes, in turn, have the ability to transport more mass than is possible via background levels of regional devolatilization. Of course, if fluids are focused into conduits, then other areas of the rock mass will be correspondingly impoverished in fluid. As a consequence, the nature and extent of mass transfer can vary significantly, even at the outcrop scale (Ague, 2007, 2011). Another reason that conduits have received so much attention is a practical one. In order to quantify chemical and isotopic changes, one needs to compare the altered rock to less-altered or unaltered equivalents. These are relatively straightforward to identify in cases of focused flow (e.g., Figure 8) but are much more challenging to assess for pervasively altered systems in which little trace of the unmodified rock remains. Rocks of the Mt. Isa Inlier provide examples of massive metasomatism on the regional scale in the shallow crust (Section 4.6.9.1.1).

Mass transfer will depend on a host of geologic variables, including P, T, fluid composition, rock composition, fluid flux, fluid transport mechanism, and tectonic setting. Consequently, generalizations must be made with great caution. Nonetheless, some broad patterns are beginning to become clear. The relative ease of transport will scale roughly with the magnitudes of elemental concentrations and concentration gradients in lithospheric fluids (Figure 24). Many commonly cited types of nonvolatile element mass transfer involve the alkali and alkaline earth metals, principally potassium, sodium, and calcium; examples are known from the shallow crust to subduction zones (e.g., Ague, 1991, 1994b, 1997a.
Another, related, type of behavior involves loss of alkali and alkaline earth metals rather than simple exchanges such as sodium–potassium or potassium–sodium. Much remains to be learned, but it is likely that these mass losses require more chemically aggressive fluids (e.g., high chlorine content), larger fluid fluxes, and/or more extreme P–T conditions than simple exchange. Loss of these metals can produce highly peraluminous rock types in which aluminous minerals, such as staurolite and Al2SiO5 polymorphs, can crystallize. Moreover, the large fluxes involved, which can reach \( \sim 10^6 \text{ m}^3 \text{ m}^{-2} \), can transport significant silica. Selverstone et al. (1991) describe silica depletions and variable alkali metal losses during up-flow in a major shear zone in the Tauern Window, eastern Alps. Down-flow in quartz veins precipitated silica and stripped alkalis from adjacent selvages, which strongly enhanced staurolite and kyanite growth in the Wepawaug Schist, Connecticut (Ague, 1994b, 2011). Overall, silica was deposited in veins by ascending, through-going fluids, but there was also substantial silica depletion from the selvages following the crack flow seal model described in Section 4.6.9.3.1. The alkali loss was due mainly to destruction of micas and plagioclase. Yardley (1986) documents retrograde alkali metasomatism and the resultant formation of aluminous mineral assemblages, including tourmaline, staurolite, garnet, and andalusite in Knockaunbaun, Ireland. Oliver et al. (1998) describe midcrustal amphibolite facies alkali and calcium loss and the growth of aluminous mineral assemblages in vein selvages related to regional fluid flow in the vicinity of the Kanmantoo ore deposit, Australia.

Major element mass transfer can be coupled to isotopic shifts that allow the fluid source to be traced. Tracy et al. (1983) found strong metasomatism, including the loss of nearly all potassium and sodium, in metacarbonate rock...
adjacent to an amphibolite facies quartz vein. The infiltrating fluid had lower \( x_{CO_2} \) than fluid in equilibrium with the wall rock and, thus, drove extensive decarbonation of the selvage (e.g., Figure 17(a)). The \( \delta^{18}O \) of the vein quartz (and selvage calcite) is lower than in metacarbonate rock beyond the selvage margins (Tracy et al., 1983), consistent with infiltration of external fluid derived from or equilibrated with syntectonic intrusions or underlying mafic metavolcanic rocks (Palin, 1992; van Haren et al., 1996).

At higher degrees of fluid–rock interaction or more extreme metamorphic conditions, elements typically considered to be inert can be mobilized at scales larger than hand samples (Figure 24). In spite of its low concentrations in typical chloride-bearing aqueous fluids, the field occurrence of aluminosilicates and other aluminum-bearing minerals in veins clearly demonstrates some degree of aluminum mobility (e.g., Austrheim, 1990; Beiter et al., 2008; Kerrick, 1990; McLelland et al., 2002; Nabelek, 1997; Whitney and Dilek, 2000; Widmer and Thompson, 2001). What is less well documented is whether the mass transfer is local- or requires larger-scale fluid flow.

Evidence to date, although limited, demonstrates that both are possible. For example, Widmer and Thompson (2001) propose that disequilibrium overstepping of reactions in wall rocks could generate large chemical potential differences between the wall rocks and precipitation sites in veins. They argue that aluminum can be mobilized locally without significant fluid flow to form kyanite-bearing segregation veins in high-\( P \) (~2.5 GPa) environments. On the other hand, mass balance studies of veins cutting amphibolite facies metapelitic and metacarbonate rocks in Connecticut (Ague, 2003, 2011) and metapelites in the Shetland Islands, Scotland (Buchholz and Ague, 2010), demonstrate aluminum addition. The selvages surrounding kyanite-bearing quartz veins in the metapelitic examples underwent aluminum mass additions. Thus, the kyanite in the veins was not derived by local aluminum loss from the surroundings; precipitation from migrating fluids was required. Aluminum gains were accompanied by silica precipitation in veins and significant alkali losses; in the Connecticut example, the added aluminum, together with the loss of alkalis, helped to stabilize selvage kyanite and staurolite. The selvage alteration is more extensive around kyanite-bearing veins than around those that are composed mostly of quartz. In the Connecticut metacarbonate rocks, the added aluminum is manifested by crystallization of minerals, such as clinozoisite, zoisite, and hornblende in vein selvages and along other conduits, including lithologic contacts.

Complexing of aluminum with aqueous silica, alkalis, and/or halogens is probably important for enhancing aluminum concentrations and facilitating aluminum transport, particularly at scales larger than local vein–wall rock systems (e.g., Diakonov et al., 1996; Manning, 2006, 2007; Manning et al., 2010; Salvi et al., 1998; Tagirov and Schott, 2001; Walther, 2001; Wohlers and Manning, 2009). Of course, aluminum is strongly mobilized during partial melting: sillimanite-rich resistites and other igneous phenomena are distinct from the fluid-driven mass transfer focused on herein.

HFSE, including REE, titanium, and zirconium, likely have very low concentrations in most lithospheric fluids. Nonetheless, there are a growing number of examples of HFSE transport (Figure 24). Most of these are from deep-crustal and subduction zone settings. For example, Gao et al. (2007) describe titanium–niobium–tantalum transport in fractures cutting eclogite facies rocks, Tianshan subduction complex, NW China. In the same orogenic belt, John et al. (2008) document LREE losses, lithium gains, and other metasomatic phenomena associated with eclogite facies veining that cuts blueschist, and van der Straaten et al. (2008) describe REE and uranium loss from eclogite that was rehydrated to form blueschist. Rubatto et al. (1999) and Rubatto (2002) interpret oscillatory-zoned zircon in a vein from an eclogitic mica schist in the Sesia-Lanzo zone to represent deposition from a fluid phase during prograde metamorphism. On the other hand, zirconium appears to be mostly inert during jadeite formation in subduction zones (Fu et al., 2010). Thorium probably has very limited mobility in fluids (e.g., Breeding et al., 2004b; Hawkesworth et al., 1997; Johnson and Plank, 1999), but uranium can be transported, particularly in relatively oxidized fluids (Hawkesworth et al., 1997). It is probable that the high-\( P \) (and in some cases \( T \)) conditions encountered in subduction settings enhances complex formation and the solubility of refractory phases, such as rutile (Antignano and Manning, 2008a; Audétat and Keppler, 2005). The wide variety of rock types juxtaposed in subduction channels, including metamorphosed ultramafic, mafic, and metasedimentary rocks, will lead to diverse metasomatic behaviors, as no single fluid will be in chemical equilibrium with all lithologies (Chapter 4.20). An important research problem is whether the HFSE transport is regional or if it occurs only at local scales; Gao et al. (2007) conclude that titanium–niobium–tantalum transport occurred over distances of at least 1 m. Given their low concentrations in fluids, mass transfer of HFSE, even at these scales, implies considerable fluid fluxes.

HFSE transport has been documented in other settings as well, including Barrovian metamorphism. For example, in the Wepawaug Schist of Connecticut, HREE addition to vein selvages is observed in both metacarbonate and metapelitic rocks. In one strongly HREE-enriched greenschist facies metacarbonate rock, the HREE are hosted in vein xenotime (see Figure 6 in Ague, 2003). In amphibolite facies metapelitic selvages surrounding quartz–kyanite veins, the HREE are hosted by garnet, which grew extensively in the selvages as a result of fluid–rock interaction (Figure 25(a); Ague, 2011). Additions of other elements to the selvages, including iron, manganese, and yttrium, also reflect this widespread garnet growth (Figure 26). Middle REE were mobile as well, leading to significant changes in, for example, Sm/Nd ratios (Figure 25(b)). In these examples, geochemical profiles across vein–wall rock contacts demonstrate that the HREE were not derived locally and must have been deposited by migrating fluids. By contrast, zirconium and titanium were essentially immobile in most rocks (Figure 26), although local depletion of titanium to form rutile in veins was observed in isolated examples. Extremely aluminous kyanite-bearing rocks from Unst, Shetland Islands, Scotland, also record limited local titanium mobility and significant REE transport (Buchholz and Ague, 2010). Here, garnet is absent from most rocks, so the REE transport fingerprint is different; REE were gained in vein selvages, with light and middle REE showing the strongest mass additions. All these examples were metamorphosed at relatively high pressures (~0.7
Mass change percentages for selvage formation

Figure 25  REE mass transfer by fluids. Geochemical profiles for rocks sampled on three separate traverses perpendicular to vein–wallrock contacts in two outcrops. Results for all three profiles are similar and are thus plotted together. Amphibolite facies metapelites, Wepawaug Schist, Connecticut, United States (Ague, 2011). (a) Lu/La ratio increases toward veins. (b) Sm/Nd ratio increases toward veins.

Figure 26  Mass changes for elements in geochemically altered selvages adjacent to amphibolite facies quartz–kyanite veins relative to little-altered schists distal to veins. Sample set described in Figure 25. Mass changes shown in red (gains) or blue (losses) statistically significant at 95% confidence level. Addition of aluminum and loss of alkalis and alkaline earths stabilized aluminous index minerals staurolite and kyanite and enhanced garnet growth. Continued growth of these minerals sequestered elements from passing fluids, leading to mass gains. Garnet incorporated iron, manganese, yttrium, and REE; staurolite incorporated iron, zinc, and lithium; staurolite, kyanite, and garnet incorporated aluminum. Breakdown of micas (mainly muscovite) led to losses of sodium, potassium, barium, LOI (loss on ignition, a proxy for volatile content), tin, and lead. Plagioclase breakdown resulted in losses of strontium, europium, and sodium. Silica lost locally due to transfer from selvages to adjacent veins (Figure 22). Mass balance demonstrates that 40–80% of the vein mass was derived locally; remainder was precipitated by through-going fluids. Modified from Ague JJ (2011) Extreme channelization of fluid and the problem of element mobility during Barrovian metamorphism. American Mineralogist 96: 333–352.
to >1.0 GPa) and, thus, complexing of HFSE with aluminum–silicon species in fluids may have enhanced refractory phase solubilities (e.g., Antignano and Manning, 2008a). Moreover, the common association of yttrium and/or phosphorus mass addition in these rocks with REE addition suggests REE transport as yttrium or phosphorus complexes (Ague, 2003, 2011; Buchholz and Ague, 2010).

Considerable confusion surrounding the scale of mass transfer has arisen in the literature, so scale issues are critical to discuss here. All elements can be mobilized on the scale of microns to thin sections during prograde or retrograde mineral reaction. Most can probably be mobile on the scale of several centimeter to decimeter scales as well, particularly in the presence of strong compositional contrasts between adjacent rock types that could be present, for example, along relic bedding planes in metasedimentary sequences or between blocks and matrix in mélange (e.g., Ague, 2003; Bebout and Barton, 2002; Brady, 1977; Dixon and Ridley, 1987; Joesten and Fisher, 1988; King et al., 2003; Thompson, 1975; Vidale, 1969; Vidale and Hewitt, 1973). In these settings, metasomatic zonation across contacts is possible if fluids are present for sufficient durations and the chemical gradients in the fluids are large enough. For thin section- to roughly decimeter-scale transport, diffusion will dominate. To move nonvolatile element mass at scales of several meters to outcrop to regional scales, however, advective fluxes will be necessary in most cases. The scale of transport, regardless of transport process, will be linked to fluid–rock partitioning behavior ($K_v$; Section 4.6.7); elements with large $K_v$ will have larger characteristic transport distances than those with small $K_v$. Consequently, even though HFSE transport may have only occurred over a few meters in a particular outcrop, the fluid flux necessary would be large, given the likely exceedingly small $K_v$. A critical point to emphasize regarding vein selvages is that, although they may only be centimeter to meter scale in thickness (Figures 8 and 22), they can line flow conduit networks stretching over kilometer scales. Thus, selvages are critical loci of interaction between regionally migrating fluids and their enclosing wall rocks, facilitating ion exchange and modifying the composition of fluids substantially along lithospheric flow paths.

The focusing of fluids into conduits can lead to strong spatial heterogeneities in flow patterns. The isotopic and chemical metasomatism recorded around conduits provides a record of large fluid fluxes and focusing. On the other hand, channelization will deprive other parts of the rock mass of fluid. In these areas, fluxes will actually be lower than expected for regional devolatilization (Zack and John, 2007). In fact, flux variations of two orders of magnitude or more are possible even on meter or decimeter scales (Figure 23; Ague, 2007, 2011). As a consequence, the mass transfer effects of regional fluid flow can be highly heterogeneous, even at the outcrop scale. Rocks far removed from veins, shear zones, lithologic contacts, and other features that may focus flow will undergo the least chemical and isotopic modification during fluid transport. Therefore, they are the best targets for studies which seek to trace the geochemistry of rocks back to their low-T origins to elucidate, for example, original sedimentary depositional environments or biomarkers of early life. Moreover, low-flux and high-flux rocks in the same outcrop will undergo different mineral reaction histories and, thus, record different parts of $P$–$T$–$t$ paths; this information will, in turn, provide multiple independent constraints on orogenic evolution.

Despite the near ubiquity of veins and other conduits in orogenic belts, the number of mass balance studies that quantify nonvolatile element mass transfer is surprisingly small. These data are necessary to integrate heterogeneous flux and mass transfer results from the outcrop scale to the regional scale.

### 4.6.9.6 Heat Transport by Fluids

Rocks conduct heat fairly readily, so fluid fluxes must be large, channelized, and/or transient for advection of heat to be important (cf. Bickle and McKenzie, 1987; Brady, 1988; Connolly and Thompson, 1989; England and Thompson, 1984; Gerya et al., 2002; Hoisch, 1991). For example, a series of ten granulite facies thermal anomalies or hot spots measuring 10–30 km$^2$ are spread out in a belt ~150 km long in part of the Acadian orogen, New Hampshire, United States (Chamberlain and Rumble, 1988). Chamberlain and Rumble (1988, 1989) proposed that the hot spot near the town of Bristol is an area where large volumes of ascending hot fluid were focused through a network of quartz veins, thereby perturbing regional thermal and oxygen isotope systematics. The large fluxes could have been achieved by focusing of fluids generated by metamorphic devolatilization or magmatic degassing into the comparatively small area of the hot spot (Brady, 1988; Chamberlain and Rumble, 1989), or by recycling fluids in a convective flow system (Chamberlain and Rumble, 1989). The timescale of flow must have been less than ~10$^6$ years; otherwise, the surroundings would have heated up, destroying the steep thermal gradients observed in the field (Brady, 1988; Chamberlain and Rumble, 1989). Another alternative is that heat was transported vertically through the hot spots mostly by magmas rather than hot fluids, although no direct evidence for such magmas has been found.

Ferry (1992) and Ague (1994b) used the dimensionless thermal Peclet number ($B$) of Brady (1988) to assess whether or not the large fluxes needed to make regional quartz vein sets elsewhere in the Acadian orogen of New England may have also transported heat:

\[
B = \frac{(d_T/\Delta t) \rho C_p L}{K_{\tau f}}
\]

in which $L$ is the length scale, $\rho C_p f$ is the product of the density and heat capacity of the fluid, $K_{\tau f}$ is the thermal conductivity of the rock, and $\Delta t$ is the total time of fluid flow. $B$ estimates the relative importance of heat transfer by advection (numerator) and conduction (denominator). For example, a $B \approx 2.7$ is obtained using the $d_T$ for the higher grade parts of the Wepawaug Schist $= 6 \times 10^4$ m$^{-3}$, a regional $L = 10$ km, $\Delta t = 10^7$ years, $K_{\tau f} = 2.5$ W m$^{-1}$ K$^{-1}$, and $\rho C_p f = 3.5 \times 10^6$ J m$^{-3}$ K$^{-1}$ (Ague, 1994b). $B > 2$ suggests a significant role for heat transport by fluid flow. Ferry (1992) came to a similar conclusion for rocks in northern New England.

These examples notwithstanding, there are relatively few documented cases of strong, fluid-driven heat transport at mid- or deep-crustal levels in orogenic belts. Modeling shows that for typical devolatilization fluxes and timescales, heat conduction will play a much larger role than fluid advection (e.g., Bickle and McKenzie, 1987; Brady, 1988; Connolly and...
Even for a comparatively large $q_{th}$ value of $10^8 \text{ m}^3 \text{ m}^{-2} \text{ yr}^{-1}$, $B$ is $<1$ for orogenic time ($10^7$ years) and length scales, and the associated temperature anomalies are only $5–15 ^\circ \text{C}$ (Lyubetskaya and Ague, 2009). It is reasonable to conclude that large, fluid-driven thermal anomalies will be limited to very high flux and/or very short timescale settings. An important research challenge is to determine how common such anomalies are in orogenic belts and assess their importance to lithospheric heat budgets.

### 4.6.9.7 Timescales of Fluid Flow

As discussed in Section 4.6.9.6 earlier, the timescale of fluid flow is critical to problems of advective heat transport by fluids. Timescales are also fundamental to fluid–rock reactions, as slow transport relative to reaction rates will favor local equilibrium, whereas fast transport and slow rates will lead to disequilibrium (Figure 15). Isotopic dating provides direct constraints on the timing and timescales of reaction. Furthermore, the preservation of isotopic or chemical disequilibrium in crystals or rocks yields important quantitative information about timescales if temperatures and rates of diffusion or recrystallization are known. For example, consider a mineral that fails to reach oxygen isotope equilibrium with an infiltrating fluid. If intracrystalline diffusion is the primary means by which the mineral interacts with the fluid, and the temperature of infiltration is known, then the maximum timescale over which the mineral and fluid were in contact can be estimated based on the degree of isotopic disequilibrium preserved in the mineral (e.g., Palin, 1992;van Haren et al., 1996; Young and Rumble, 1993). If complete equilibration is achieved, then only minimum timescales can be estimated. There are many other ways to use transport–reaction theory to estimate rates; Skelton (2011) provides a current example. Dating of the growth histories of porphyroblasts, such as garnet, does not, in and of itself, provide direct constraints on fluid presence or absence. However, most garnet-producing reactions liberate water, so the age ranges provide insights into the timescales of fluid presence in a dewatering rock mass.

The range of timescales relevant to fluid–rock processes in the crust spans at least six orders of magnitude (Figure 27). Some of the shortest timescales of fluid infiltration are found in and around veins, shear zones, and subduction zone mélanges. Timescales are typically less than a few thousand years; some studies calculate that individual events in some geological settings can be as short as 10–100 years! These results are consistent with highly pulsed, transient fluid or thermal regimes associated with deformation and may, in some cases, reflect hydrofracturing, rapid seismic moment release, or the passage of porosity waves. Some metacarbonate rocks also preserve evidence for short timescales of fluid–rock interaction. It is possible that extremely low rock permeabilities limited the amount of fluid infiltration and, thus, the timescales of reaction.

It is important to emphasize that the short timescales for veins and other settings shown in Figure 27 need not represent the total span of time over which fluid activity occurred. For example, say there were five pulses of fluid flow, each lasting $10^4$ years, spaced 1 My apart. The total integrated timescale for direct fluid–rock interaction would be 50 000 years, but the activity occurred over a $\sim 4$ Ma time interval. Most diffusion-based methods will estimate the 50 000 year integrated timescale; isotopic dating is needed to pin down the longer time interval (e.g., Camacho et al., 2005; Pollington and Baxter, 2010).

Available timescale estimates for regions that undergo large-scale, pulsed thermal events are on the order of a few hundred thousand to a few million years (e.g., (g), (h), (k), (m), and (n) in Figure 27). In a number of cases, direct links to advective emplacement of syn-metamorphic magmas can be made, but other heat sources, including heating from viscous deformation (e.g., shear zones) and fluid flow, may also be important. Timescales will reflect both rates of advection and of conduction away from advective heat sources.

In the Barrovian type locality, Scotland, Baxter et al. (2002) determined precise Sm/Nd ages for garnet growth which, when combined with the age data of Oliver et al. (2000), indicate a total time span of $\sim 8$ Ma for garnet crystallization (Figure 27). However, the difference in peak (maximum) $T$ attainment between the garnet and sillimanite zones was only 2.8 ± 3.7 Ma ($\sigma$; statistically indistinguishable from 0). This short time span ($\sim 464–468$ Ma) is inconsistent with the larger intervals predicted by conductive thermal relaxation of variably overthickened crust (e.g., Thompson and England, 1984) and strongly suggests the involvement of an additional, advective component of heat transfer. Modeling of chemical diffusion in garnet and apatite indicates that the pulse or pulses of peak heating were of brief integrated duration, probably on the order of $10^6$ years or less (Ague and Baxter, 2007; Vorhies and Ague, 2011). There could have been one large pulse of this duration or a series of shorter pulses spread out over a longer interval of time. Baxter et al. (2002) and Ague and Baxter (2007) concluded that considerable advective heat was supplied by syn-metamorphic magmas (e.g., the Newer Gabbros), although shear zones (Vie et al., 2011) and hydrothermal fluids, perhaps exsolved from the crystallizing intrusions, may have also played a role. The total timescale of Barrovian metamorphism was 10–15 Ma (e.g., Dewey, 2005), but pulsed heating to peak conditions, and the associated fluid release, was likely to have been more transient. It is worthwhile to note that Barrow himself first proposed (1893) that intrusions provided, at least in part, the heat required for metamorphism.

The longest timescales in Figure 27 ($\sim 10^7$ year) are for extended periods of garnet growth; these timescales are comparable to those expected for large-scale orogenic events. It is not known if the garnets grew slowly and continuously over these time intervals or if growth occurred in a series of shorter pulses spread out over longer periods of time. Long-timescale growth and slow fluid release during the course of orogeny would be consistent with classical models of thermal relaxation of thickened crustal sections (e.g., England and Thompson, 1984). Even so, if devolatilization reactions are limited to narrow $P$–$T$ windows in a given bulk composition, then the duration of fluid generation and flow may be far less than that for the total orogeny. For example, Skelton (2011) concludes that fluid flow associated with regional greenschist facies metamorphism in the southwestern Scottish Highlands may have lasted only $\sim 4000$ years.

A growing body of evidence suggests that geologically brief pulses of fluid activity associated with deformation (e.g.,
fracturing and shear zones) or advective thermal pulses can be part of much longer orogenic cycles lasting 10^7 years or more. If a thermal pulse is generated due to, for example, deep regional magma intrusion, then dehydration will be rapid, potentially generating high fluid pressures, hydrofracturing, transient fluid flow, and seismicity (e.g., Lyubetskaya and Ague, 2010). Determination of fluid–rock interaction timescales is an evolving research frontier that will advance along with continued improvements in isotopic dating techniques and new diffusion coefficient calibrations.

4.6.9.8 Fluids in the Granulite Facies

Phase relations and fluid inclusion evidence indicate greatly reduced water activity (a_{H_2O}) in the granulite facies (e.g., Aranovich and Newton, 1996, 1997, 1998; Crawford and Hollister, 1986; Frost and Frost, 1987; Lamb and Valley, 1984; Newton, 1995, and numerous references cited within these papers). Concentrated aqueous solutions of strong electrolytes, including [Na and K]Cl, would have low a_{H_2O} as would CO_2-rich fluids. If both chlorine and CO_2 contents are high, then it is

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**Figure 27** Selected published timescales relevant for fluid processes: (a) Penniston-Dorland et al. (2010) and John et al. (2012); (b) Palin (1992); (c) Skelton (2011); (d) van Haren et al. (1996); (e) Young and Rumble (1993); (f) Camacho et al. (2005). Total time span of orogenic activity ~13 Ma: (g) Chamberlain and Rumble (1989); (h) Baxter et al. (2002) for total garnet growth duration, and Ague and Baxter (2007) for thermal pulse activity; (i) Bickle and Baker (1990); (j) Pollington and Baxter (2010); (k) Lancaster et al. (2008); (l) Baldwin et al. (1993); (m) Wijbrans and McDougall (1985, 1988); (n) Page et al. (2010); (o) Christensen et al. (1989); (p) Christensen et al. (1994); (q) Lapen et al. (2003).
likely that immiscible CO2-rich and chlorine-rich fluids would coexist at high P and T (Duan et al., 1995; Schmidt and Bodnar, 2000), consistent with fluid inclusion evidence for multiphase granulite facies fluids (Crawford and Hollister, 1986; Touret, 1985). The flow of dense, CO2-rich fluid would be limited by the inability of CO2 to wet grain boundaries effectively, unlike chlorine-rich brines (Watson and Brenan, 1987). Consequently, brines are probably more effective deep-crustal transport agents and have the potential to cause metasomatic effects, including alkali metasomatism and regional rubidium depletion owing to their high chlorine contents and alkali exchange capacities (e.g., Harlov et al., 1997; Smit and Van Reenen, 1997). Nonetheless, direct expulsion of CO2 from crystallizing intrusions could lower aH2O dramatically, promote granulite facies metamorphism, and, in some cases, result in graphite precipitation (Farquhar and Chacko, 1991). A variety of mechanisms for generating low aH2O fluids have been proposed, including infiltration of connate brines or fluids equilibrated with metavaporites, loss of H2O to anatectic melts (e.g., Valley et al., 1990), which can leave behind residual fluids enriched in salts and CO2 (Fyfe, 1973; Philippot, 1993), release of brines and CO2 from deep-crustal intrusions (Hansen et al., 1995), and loss of H2O to retrograde rehydration reactions (Markl et al., 1998).

4.6.10 Concluding Remarks

The concerted efforts of a diverse spectrum of Earth scientists have made it possible to estimate the amounts of fluid that flow through the continental lithosphere during mountain building and constrain the processes, timescales, and directions of fluid motion. Progress to date has been substantial, but many fundamental questions remain. For example, how deep do surficial waters penetrate into metamorphic belts? How do large fluid fluxes modify the chemical and isotopic composition of the crust and influence regional thermal structure? What are the directions and fluxes of fluid in deeply subducted crust and ultrahigh-pressure metamorphic rocks? What fraction of this deep fluid enters the mantle (see Chapter 3.11), and how does it influence the chemistry and isotopic systematics of mantle-derived melts? Time-integrated fluxes can be estimated, but over what timescales are the fluids evolved? Is the devolatilization slow and continuous, or rapid and pulsed? Rapid CO2 release, for instance, may perturb the climate system toward higher global average temperatures (Kerrick and Caldeira, 1998), whereas long-term sequestering of CO2 may lead to cooling (Selverstone and Gutzler, 1993). Emerging evidence indicates that rapid CO2 release from both contact metamorphic (Svensen and Jamtveit, 2010) and regional metamorphic (Skelton, 2011) environments may play significant roles in global carbon cycling.

Acknowledgments


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